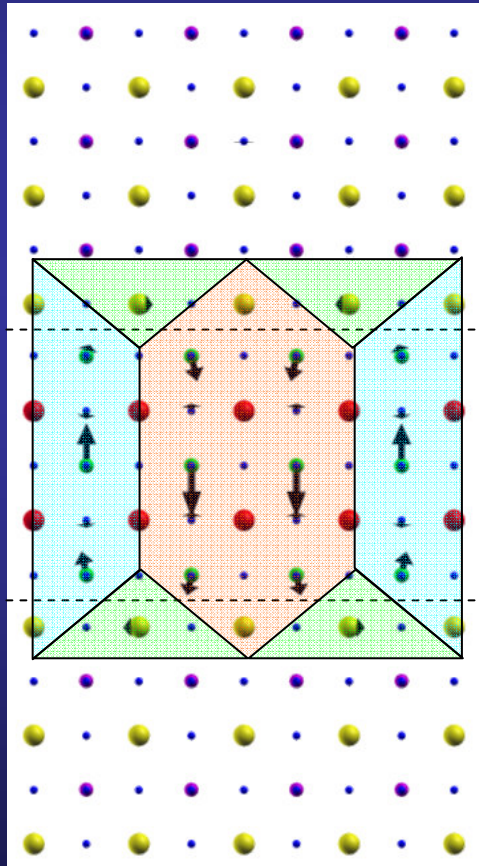


# Ferromagnetic like closure domains in ferroelectric ultrathin films



Pablo Aguado-Puente

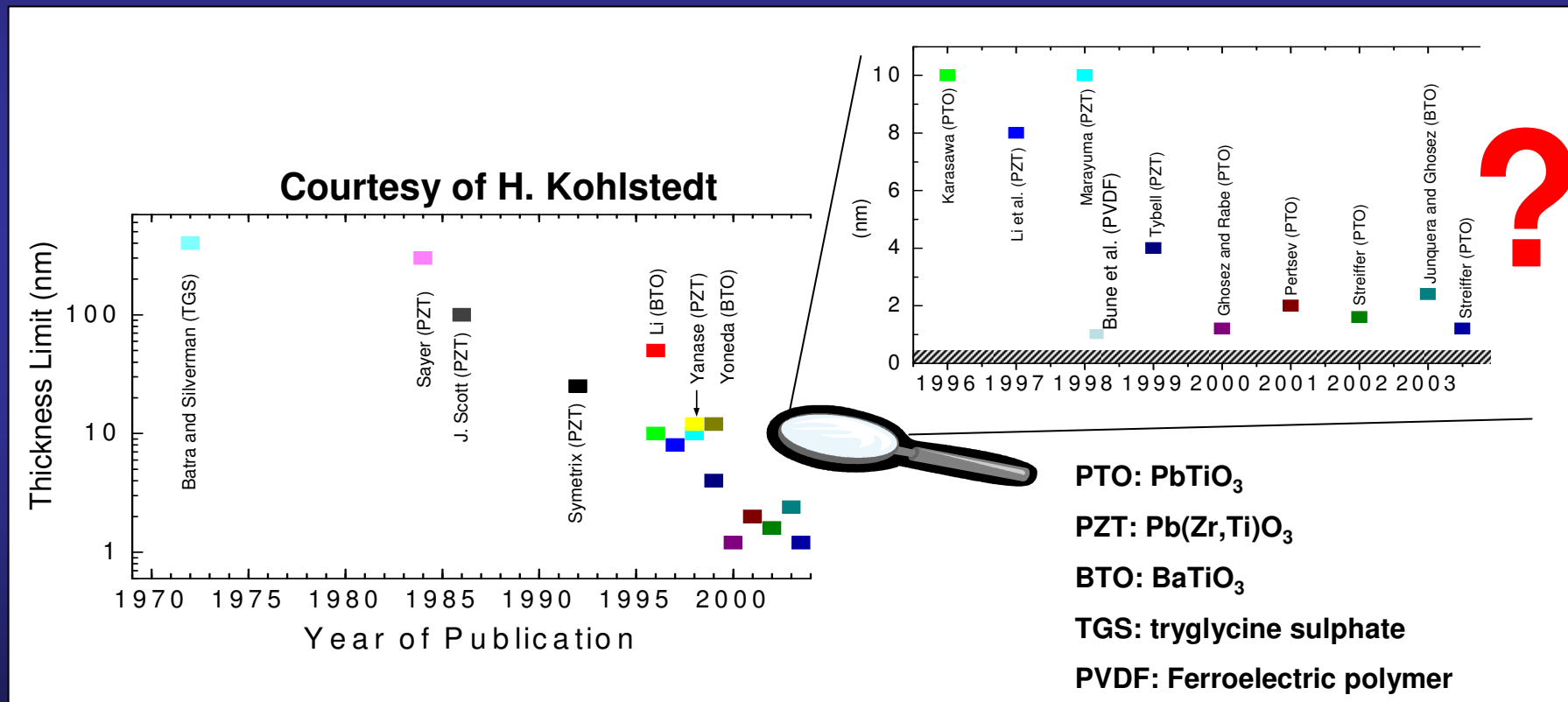
Javier Junquera



# Fundamental motivation: what's the most stable phase for epitaxial ferroelectric ultrathin films?

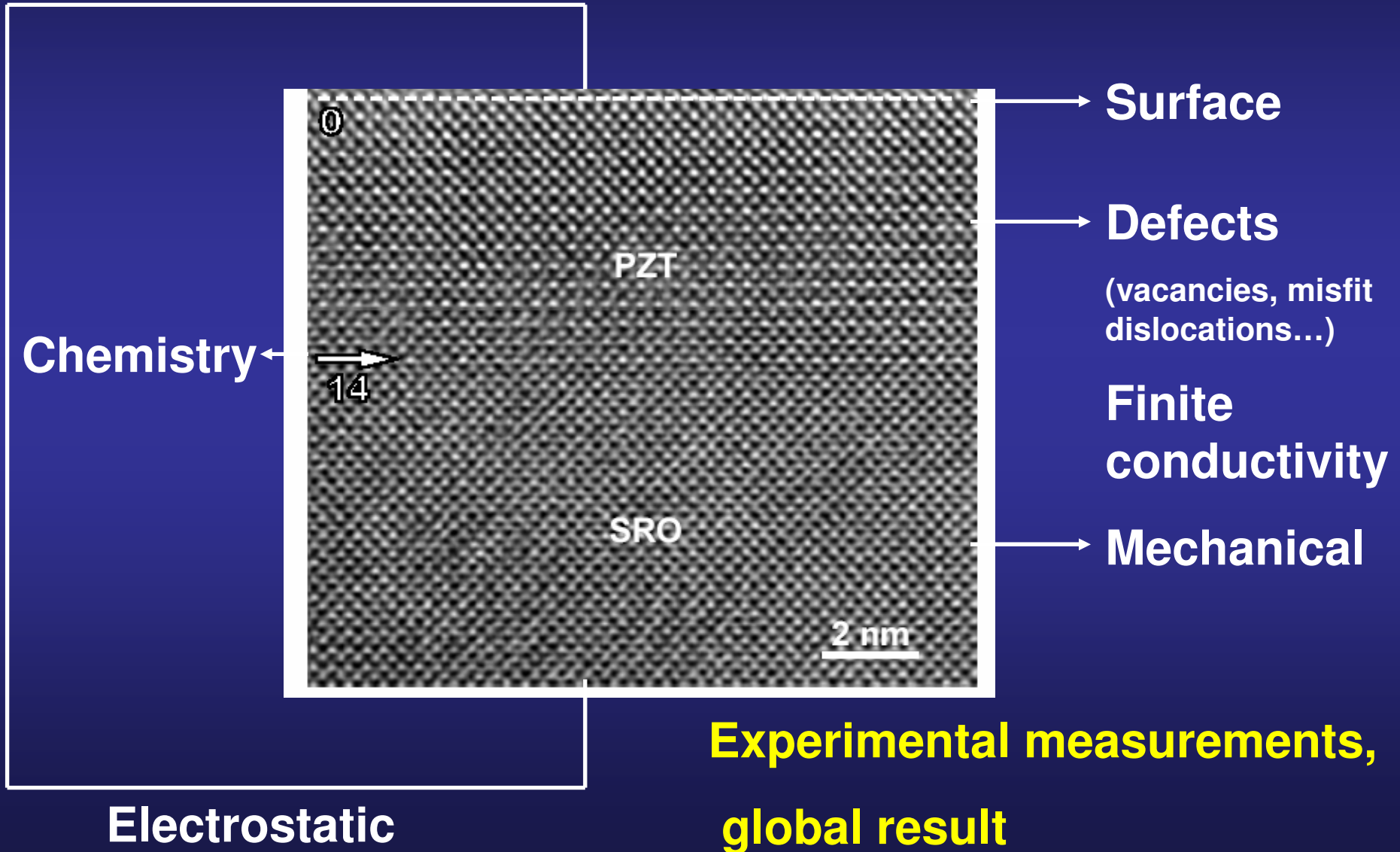
Long time question.

Hot field.

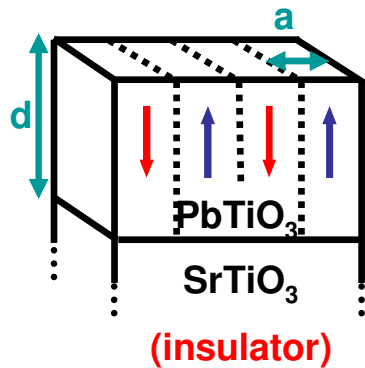


Ph. Ghosez and J. Junquera, *First-Principles Modeling of Ferroelectric Oxide Nanostructures*, *Handbook of Theoretical and Computational Nanotechnology*, Vol. 9, Chap. 13, 623-728 (2006) (<http://xxx.lanl.gov/pdf/cond-mat/0605299>) and references therein.

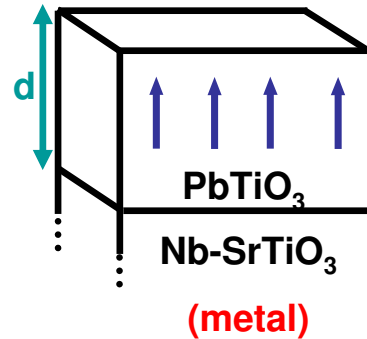
# Many effects might alter the delicate balance between long and short range forces



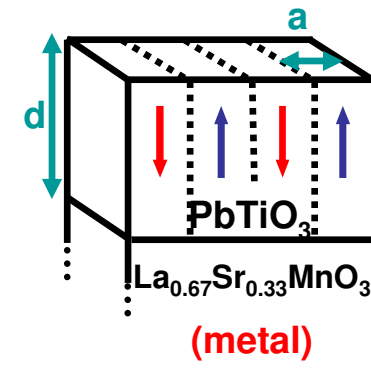
# Experimentally: small changes in boundary conditions, great changes in stable state



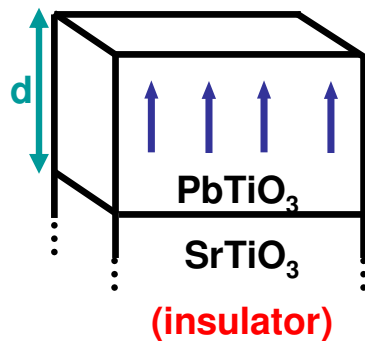
D. D. Fong et al. (2004)  
S. K. Streiffer et al. (2002)



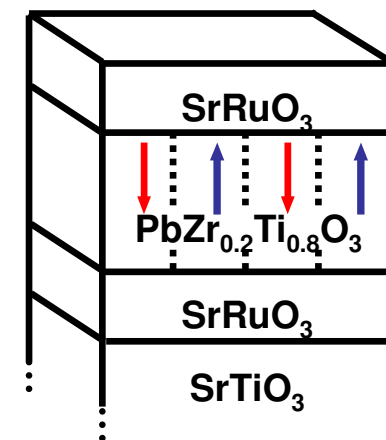
C. Lichtensteiger et al. (2005)  
A. T. J. van Helvoort et al. (2005)



C. Lichtensteiger et al. (2007)

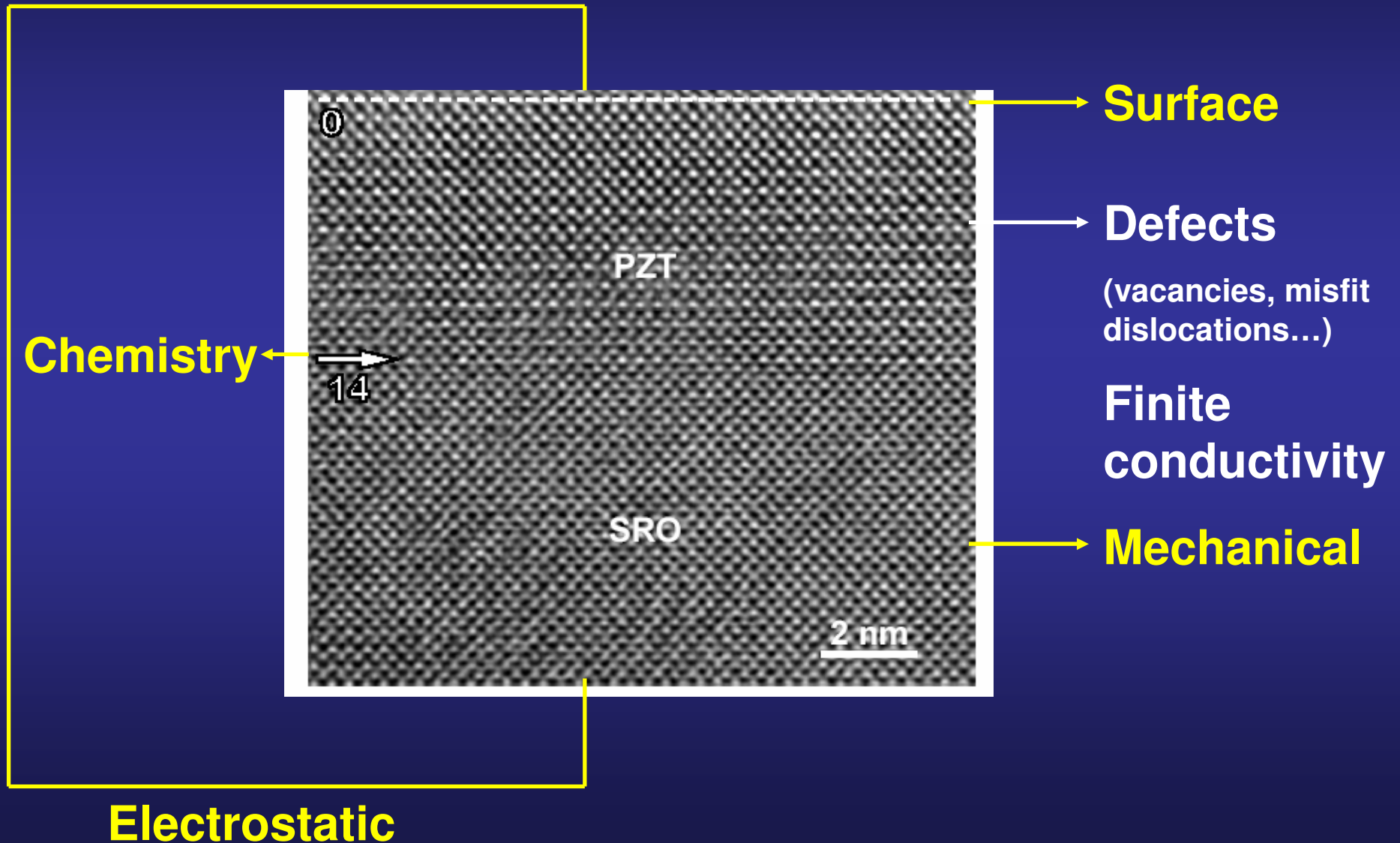


D. D. Fong et al. (2005)



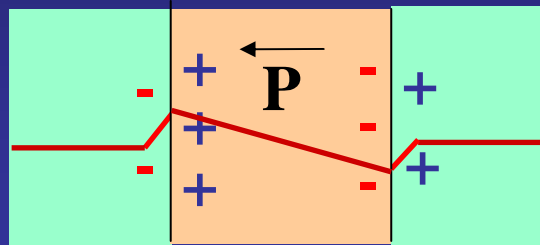
V. Nagarajan et al. (2006)

# First-principles calculations allow to isolate their respective influence



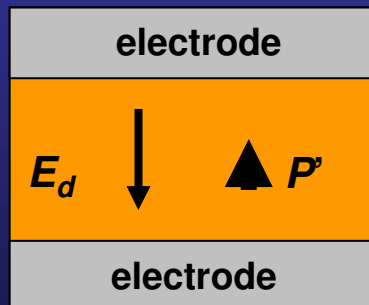
# Residual depolarizing field increases electrostatic energy and opposes to a polarization

## Real electrodes imperfect screening

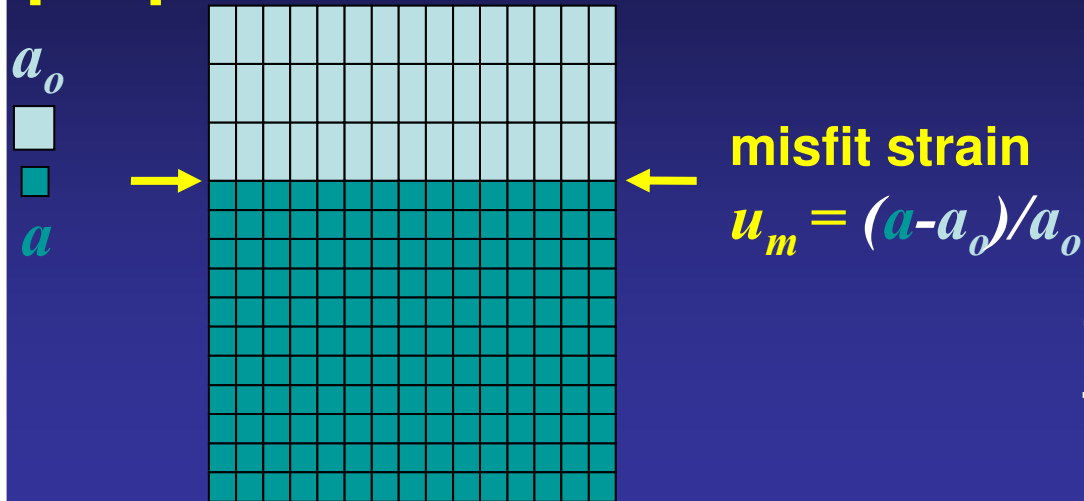


$$\mathcal{E}_d = -4 \pi [2 \cdot \lambda_{eff} / d] \cdot \mathbf{P}$$

Screening by free charges  
(electrodes or adsorbates)



# Strain imposed by the substrate affects the properties of ferroelectric materials

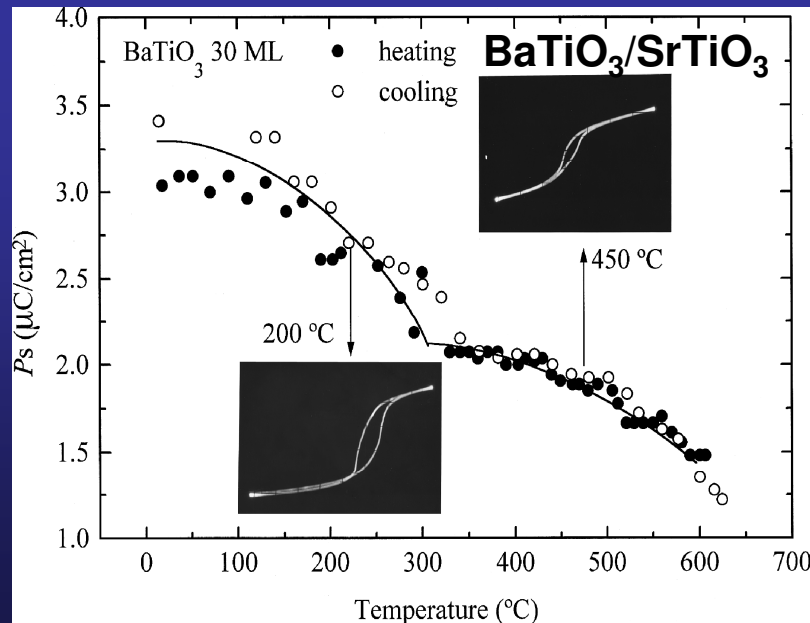


Courtesy of O. Diéguez

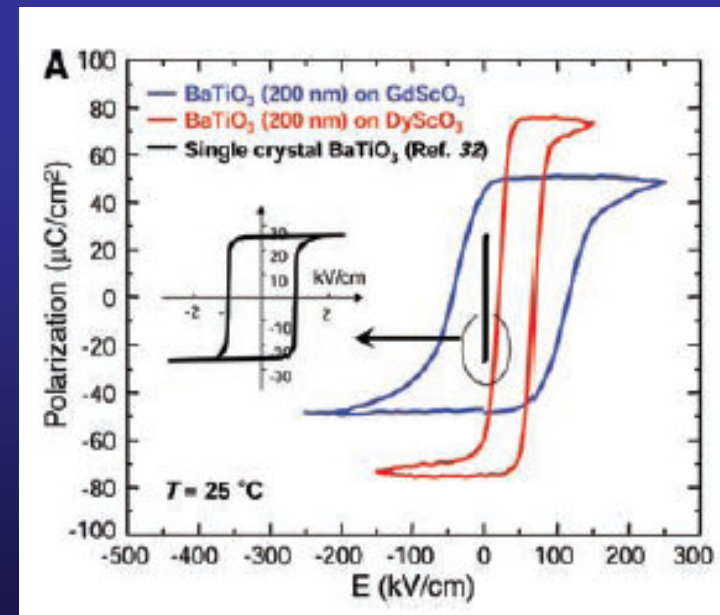
Typical picture:

Compressive strain  $\Rightarrow$  tetragonal  $c$

Tensile strain  $\Rightarrow$  orthorrombic  $aa$

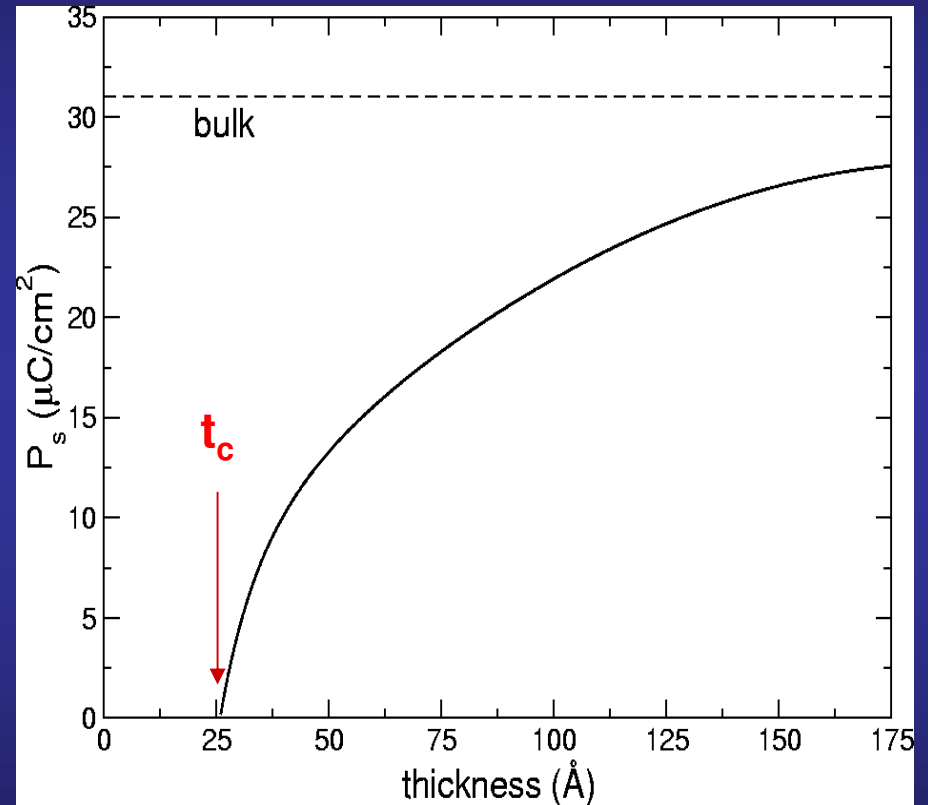
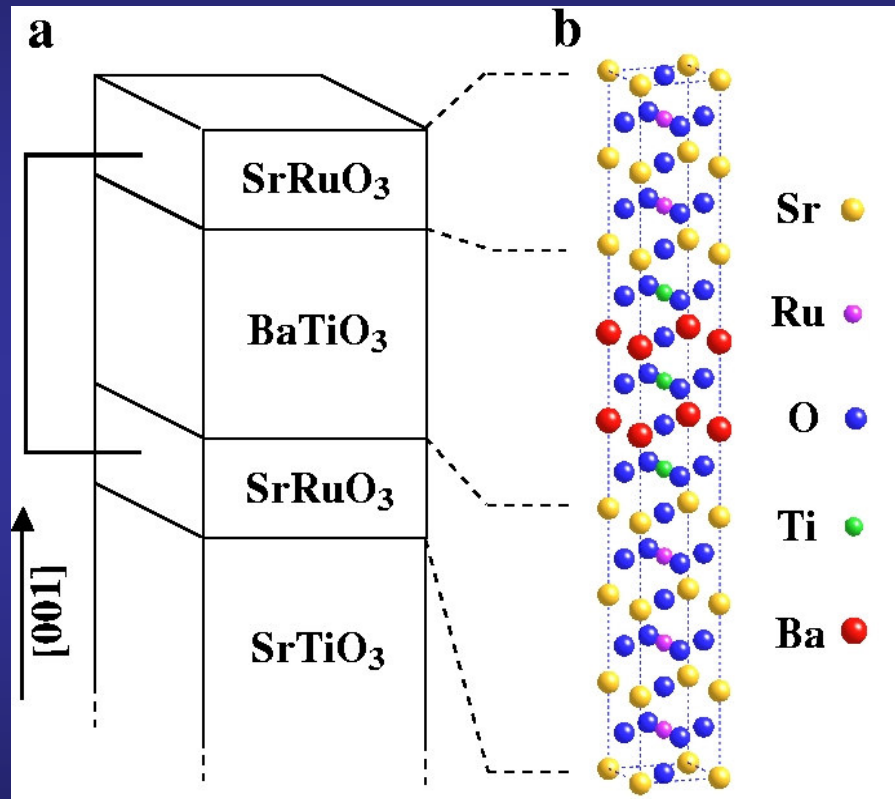


Yoneda *et al.*, J. Appl. Phys. 83, 2458 (1998)



K. J. Choi *et al.*, Science 306, 1005 (2004)

# Simulations of ferroelectric nanocapacitors from first-principles



J. Junquera and Ph. Ghosez, Nature 422, 506 (2003)



# Many DFT first-principles computations on size effects in *monodomain* ferroelectric ultrathin films

PHYSICAL REVIEW B 72, 020101(R) (2005)

## Ferroelectricity in ultrathin perovskite films

Na Sai, Alexie M. Kolpak, and Andrew M. Rappe

PRL 96, 107603 (2006)

PHYSICAL REVIEW LETTERS

week ending  
17 MARCH 2006

## Ionic Polarizability of Conductive Metal Oxides and Critical Thickness for Ferroelectricity in BaTiO<sub>3</sub>

G. Gerra,<sup>1,\*</sup> A. K. Tagantsev,<sup>1</sup> N. Setter,<sup>1</sup> and K. Parlinski<sup>2</sup>

PHYSICAL REVIEW B 74, 060101(R) (2006)

## *Ab initio* study of the critical thickness for ferroelectricity in ultrathin Pt/PbTiO<sub>3</sub>/Pt films

Yoshitaka Umeno,<sup>1,2</sup> Bernd Meyer,<sup>3</sup> Christian Elsässer,<sup>4,1</sup> and Peter Gumbsch<sup>1,4</sup>

## Interface Effect on Ferroelectricity at the Nanoscale

Chun-Gang Duan,<sup>†,‡,§</sup> Renat F. Sabirianov,<sup>†,§</sup> Wai-Ning Mei,<sup>†,§</sup>  
Sitaram S. Jaswal,<sup>†,§</sup> and Evgeny Y. Tsybal<sup>\*,†,§</sup>

NANO  
LETTERS

2006  
Vol. 6, No. 3  
483–487

PRL 96, 127601 (2006)

PHYSICAL REVIEW LETTERS

week ending  
31 MARCH 2006

## Stabilization of Monodomain Polarization in Ultrathin PbTiO<sub>3</sub> Films

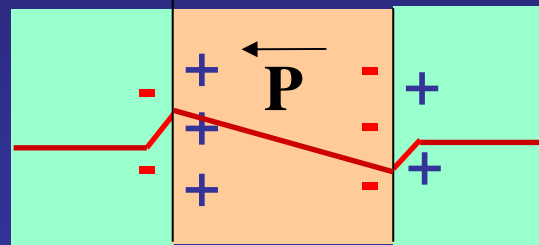
D. D. Fong,<sup>1</sup> A. M. Kolpak,<sup>2</sup> J. A. Eastman,<sup>1</sup> S. K. Streiffer,<sup>1</sup> P. H. Fuoss,<sup>1</sup> G. B. Stephenson,<sup>1</sup> Carol Thompson,<sup>3</sup>  
D. M. Kim,<sup>4</sup> K. J. Choi,<sup>4</sup> C. B. Eom,<sup>4</sup> I. Grinberg,<sup>2</sup> and A. M. Rappe<sup>2</sup>

# Many DFT first-principles computations on size effects in *monodomain* ferroelectric ultrathin films

Reference	Heterostructure	Method	Functional	Interface	$a_{  }$	$t_c$
Junquera <i>et al.</i> [56]	SrRuO <sub>3</sub> /BaTiO <sub>3</sub> /SrRuO <sub>3</sub>	NAO	LDA (CA)	SrO-TiO <sub>2</sub>	3.874 Å ( $a_{\text{SrTiO}_3}^{\text{th}}$ )	6
Junquera <i>et al.</i>	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /SrRuO <sub>3</sub>	NAO	LDA (CA)	SrO-TiO <sub>2</sub>	3.874 Å ( $a_{\text{SrTiO}_3}^{\text{th}}$ )	6
Gerra <i>et al.</i> [63]	SrRuO <sub>3</sub> /BaTiO <sub>3</sub> /SrRuO <sub>3</sub>	PW	GGA (PW91)	SrO-TiO <sub>2</sub>	3.94 Å ( $a_{\text{SrTiO}_3}^{\text{th}}$ )	3
Umeno <i>et al.</i> [89]	Pt/PbTiO <sub>3</sub> /Pt	MBPP	LDA (CA)	Pt-PbO	3.845 Å ( $a_{\text{SrTiO}_3}^{\text{th}}$ )	4
				Pt-TiO <sub>2</sub>		6
			GGA (PW91)	Pt-PbO	3.905 Å ( $a_{\text{PbTiO}_3}^{\text{exp}}$ )	No
				Pt-TiO <sub>2</sub>		No
Duan <i>et al.</i> [86]	SrRuO <sub>3</sub> /KNbO <sub>3</sub> /SrRuO <sub>3</sub>	PW	LDA (CA)	SrO-NbO <sub>2</sub>	3.905 Å ( $a_{\text{SrTiO}_3}^{\text{exp}}$ )	4
	Pt/KNbO <sub>3</sub> /Pt			Pt-NbO <sub>2</sub>		2
Na Sai <i>et al.</i> [64,90]	SrRuO <sub>3</sub> /BaTiO <sub>3</sub> /SrRuO <sub>3</sub>	PW	GGA	SrO-TiO <sub>2</sub>	3.991 Å ( $a_{\text{BaTiO}_3}^{\text{exp}}$ )	> 4
				RuO <sub>2</sub> -BaO		> 4
	Pt/BaTiO <sub>3</sub> /Pt			Pt-TiO <sub>2</sub>		> 4
				Pt-BaO		> 4
	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /SrRuO <sub>3</sub>			SrO-TiO <sub>2</sub>	3.905 Å ( $a_{\text{PbTiO}_3}^{\text{exp}}$ )	No
				RuO <sub>2</sub> -PbO		No
	Pt/PbTiO <sub>3</sub> /Pt			Pt-TiO <sub>2</sub>		No
				Pt-PbO		No
D. D. Fong <i>et al.</i> [47]	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /vacuum	PW	GGA	SrO-TiO <sub>2</sub>	$a_{\text{PbTiO}_3}^{\text{th}}$	> 3
	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /OH, O or H					< 3
	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /CO <sub>2</sub>					~ 3
	SrRuO <sub>3</sub> /PbTiO <sub>3</sub> /H <sub>2</sub> O					> 3

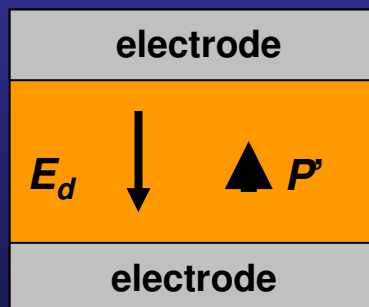
# Until today, monodomain studies, goal of this work: multidomain simulations

Real electrodes  
imperfect screening

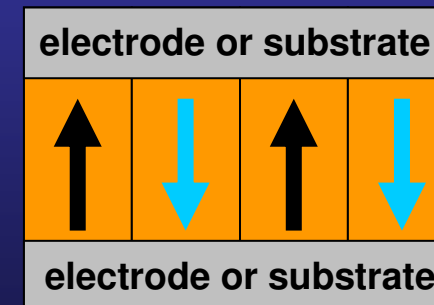


$$\mathcal{E}_d = -4 \pi [2 \cdot \lambda_{eff} / d] \cdot \mathbf{P}$$

Screening by free charges  
(electrodes or adsorbates)



Formation of domains  
(no net charge at surface)



Goal of this work

# Main questions addressed in this work

- Is the phase transition as a function of thickness from...  
homogeneous polarization to paraelectric?  
homogeneous polarization to inhomogeneous polarization?

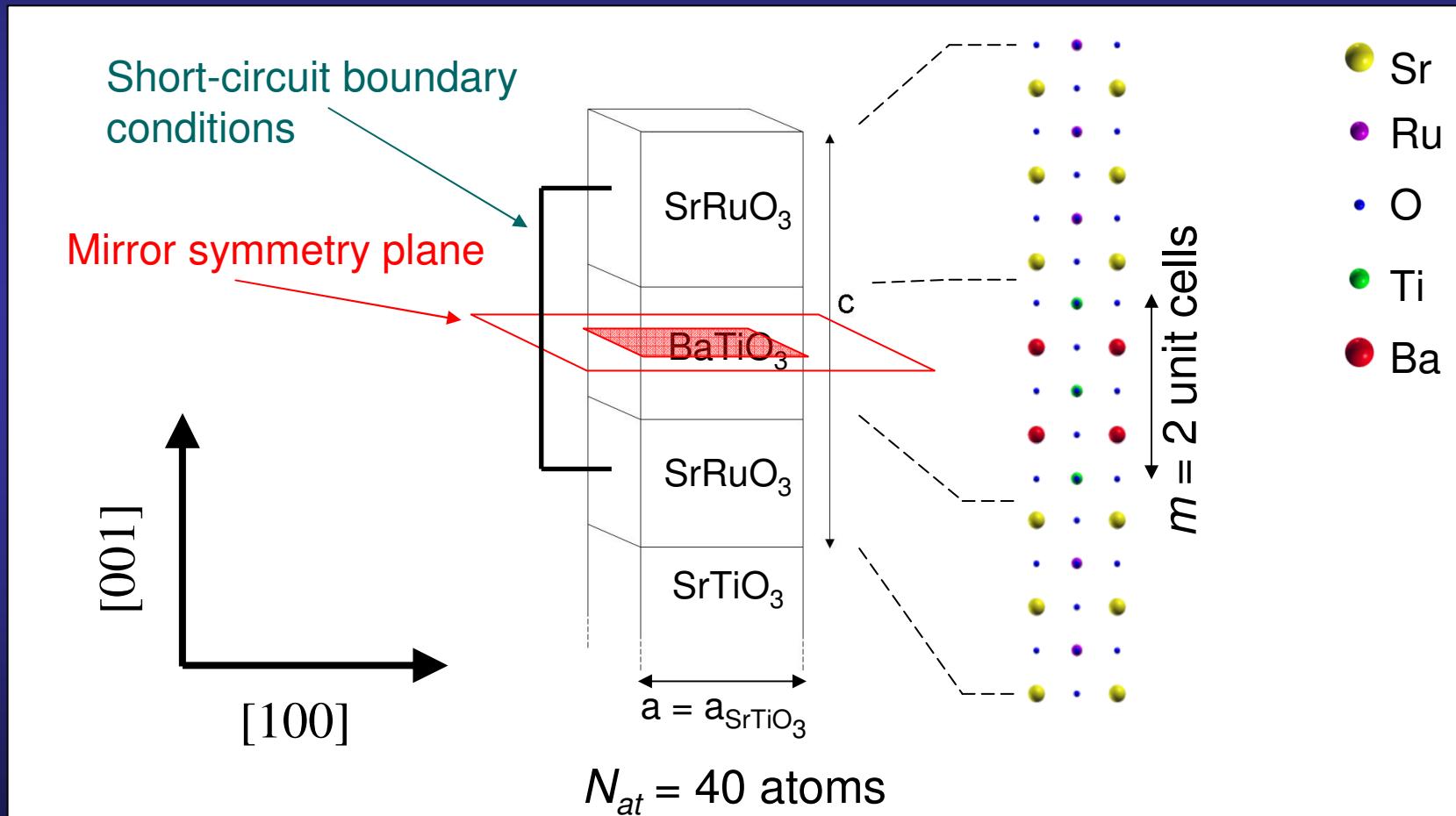
“It is not certain yet whether this instability in a single-domain ground state results in paraelectricity or in many small domains”

J. F. Scott, J. Phys.: Condens. Matter 18, R361 (2006)

- If the second is true, do the domains have a defined structure?

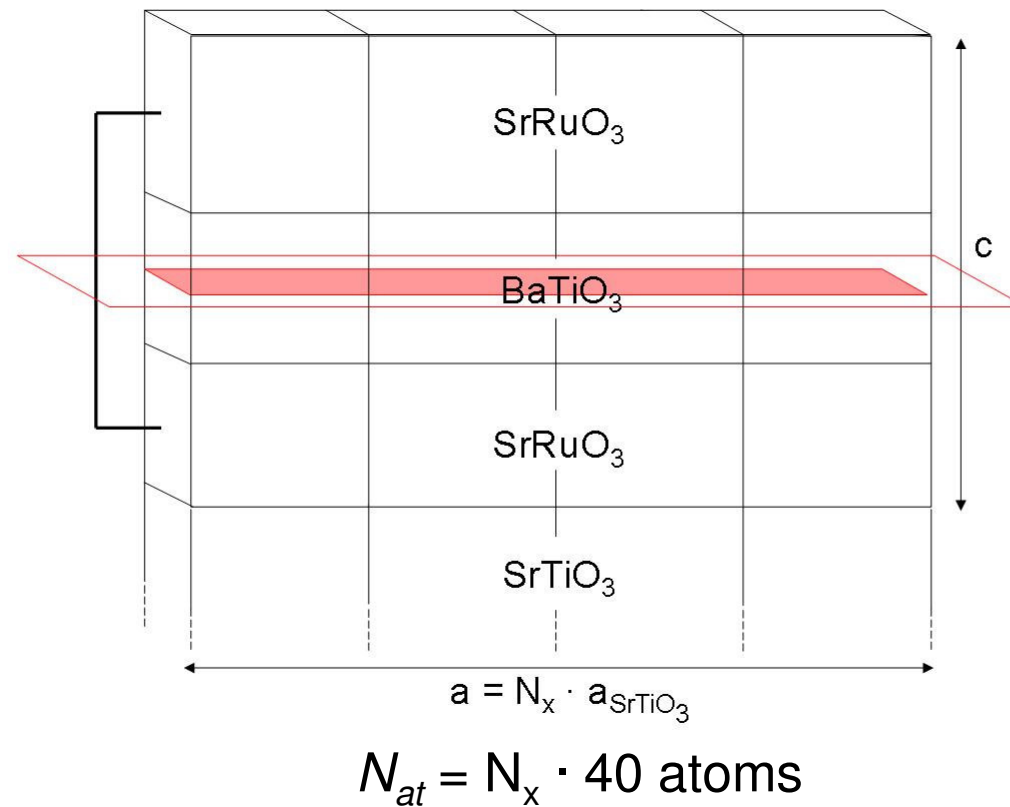
# Building the cell: the paraelectric unit cell

- Building the reference cell following the scheme of Junquera and Ghosez (2003).



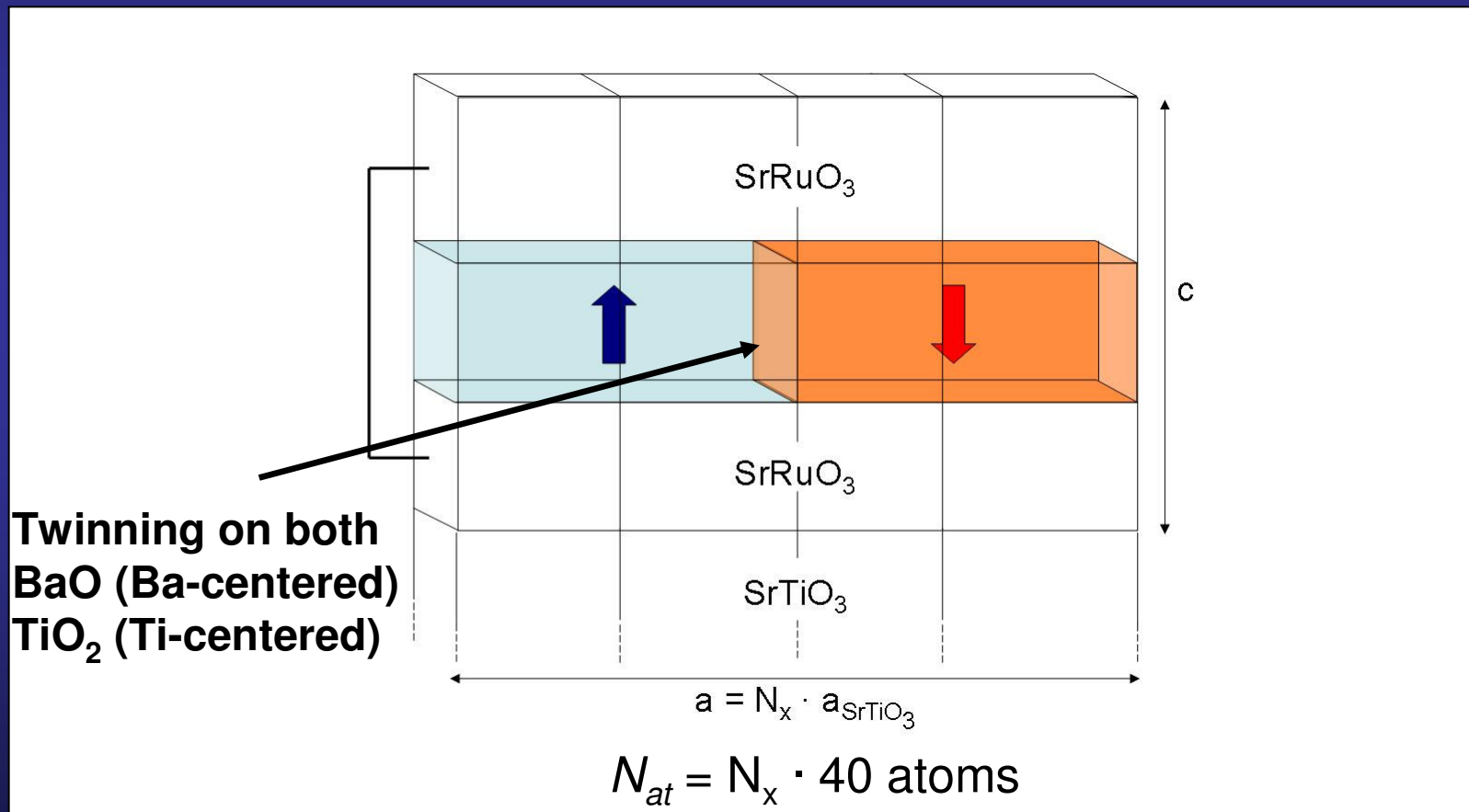
# Building the cell: replicating the paraelectric structure

- $N_x$  repetitions in [100] direction.
- The energies of these cells as references.



# Building the cell: inducing a polarization by hand

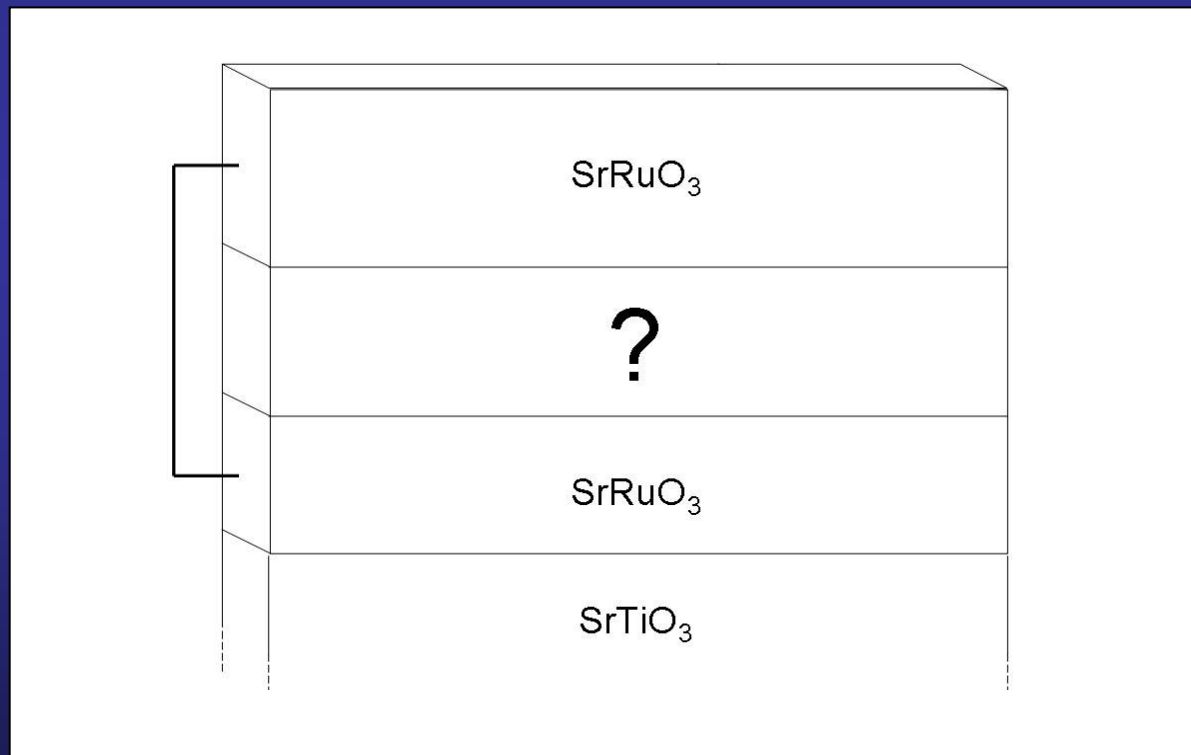
- Choosing a domain wall.
- Inducing a polarization by hand in the FE layer displacing the atoms a percentage of the bulk soft mode.



# Relaxing all the atomic coordinates, both in the ferroelectric layer and the electrodes

Forces smaller than  $0.01 \text{ eV/\AA}$

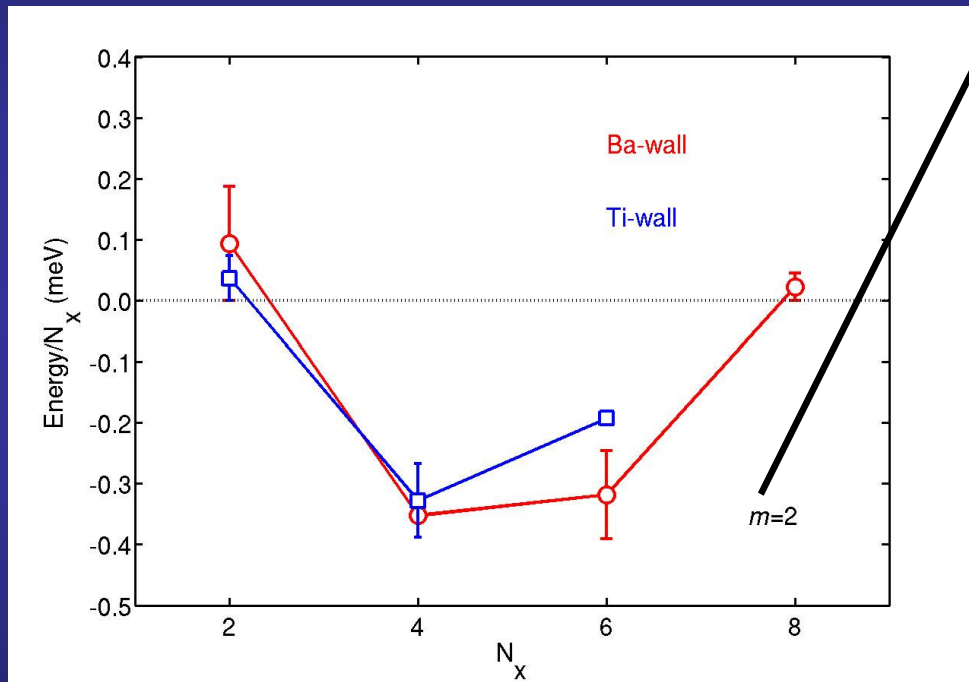
**No constraints imposed on the atomic positions**





# Polydomain phases more stable than paraelectric structure for $2 < N_x < 8$

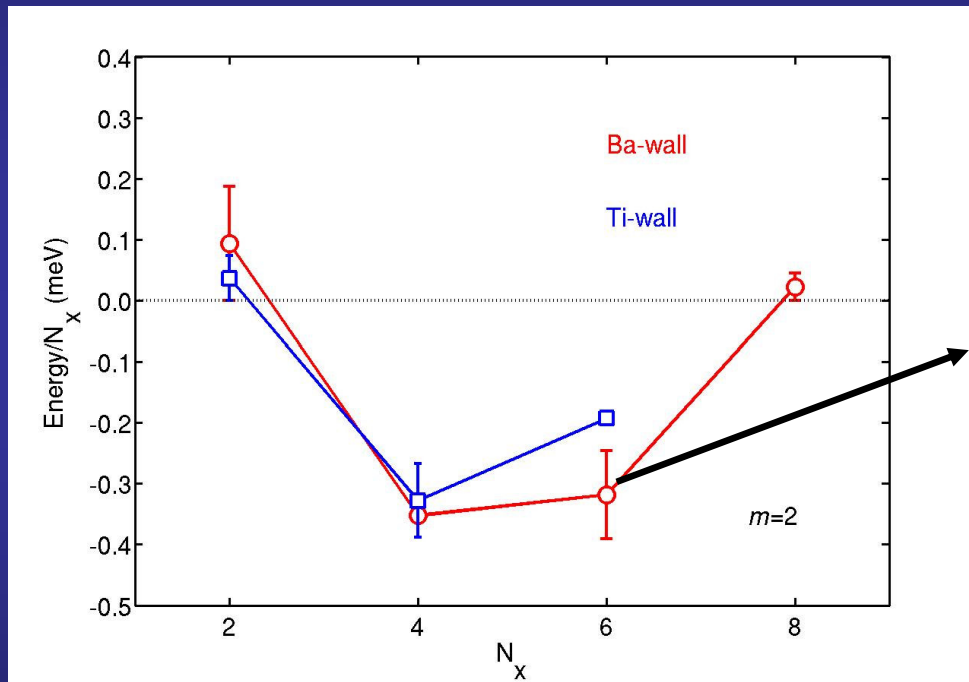
2-unit-cells thick BaTiO<sub>3</sub> layer



Polar domains stabilized below critical thickness for the monodomain configuration

# Polydomain phases more stable than paraelectric structure for $2 < N_x < 8$

2-unit-cells thick  $\text{BaTiO}_3$  layer

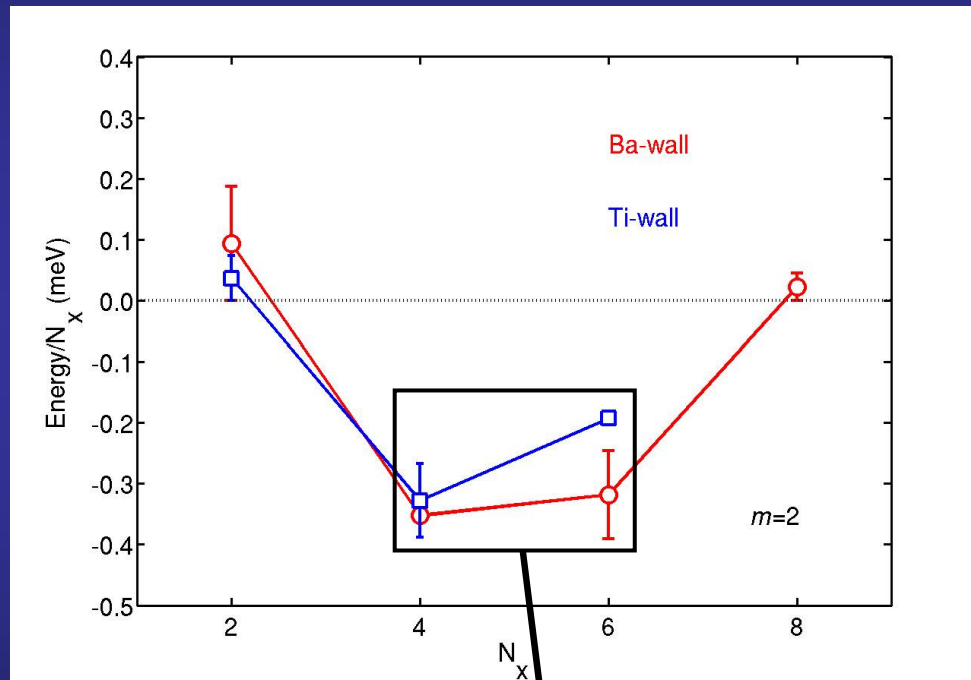


Polar domains stabilized below critical thickness for the monodomain configuration

As  $180^\circ$  domains in bulk,  
Ba centered domain wall preferred

# Polydomain phases more stable than paraelectric structure for $2 < N_x < 8$

2-unit-cells thick BaTiO<sub>3</sub> layer



Polar domains stabilized below critical thickness for the monodomain configuration

As 180° domains in bulk,  
Ba centered domain wall preferred

No energy difference between  $N_x = 4$  and  $N_x = 6$

Both of them might be equally present in an sample

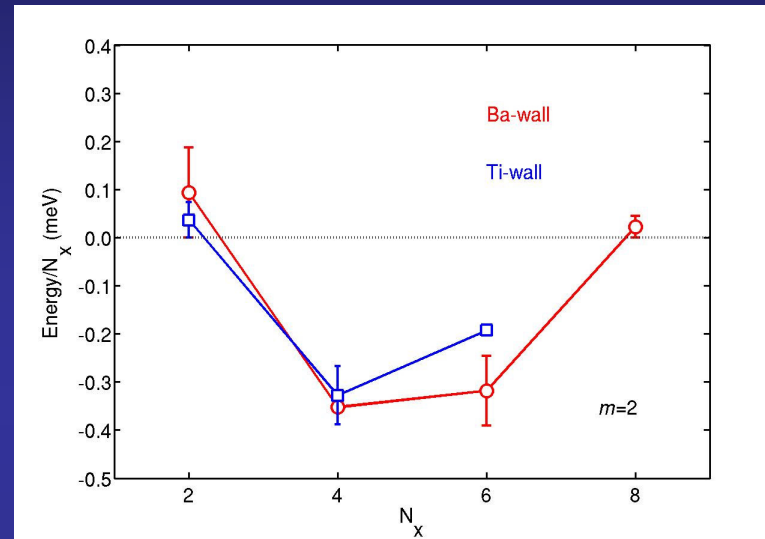
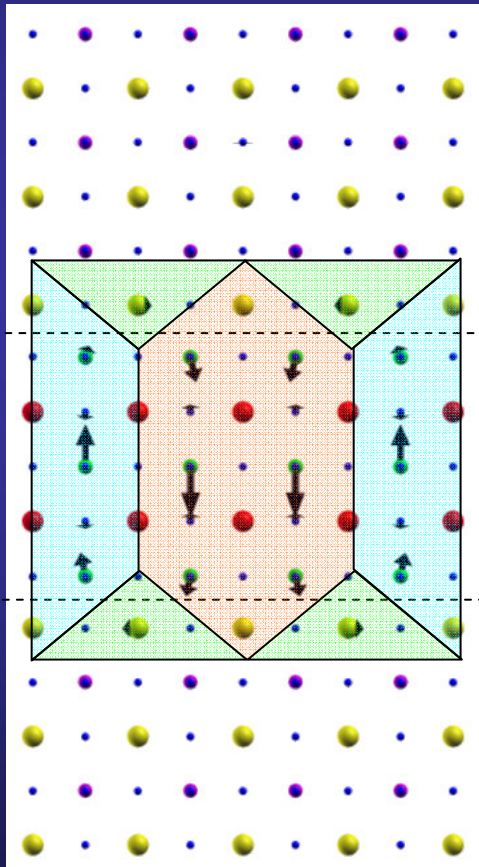
( $\alpha$  and  $\beta$  phases in PbTiO<sub>3</sub>/SrTiO<sub>3</sub> interfaces?)

D. D. Fong *et al.*, Science 304, 1650 (2004)

# Polydomain phases adopt the form of a “domain of closure”, common in ferromagnets

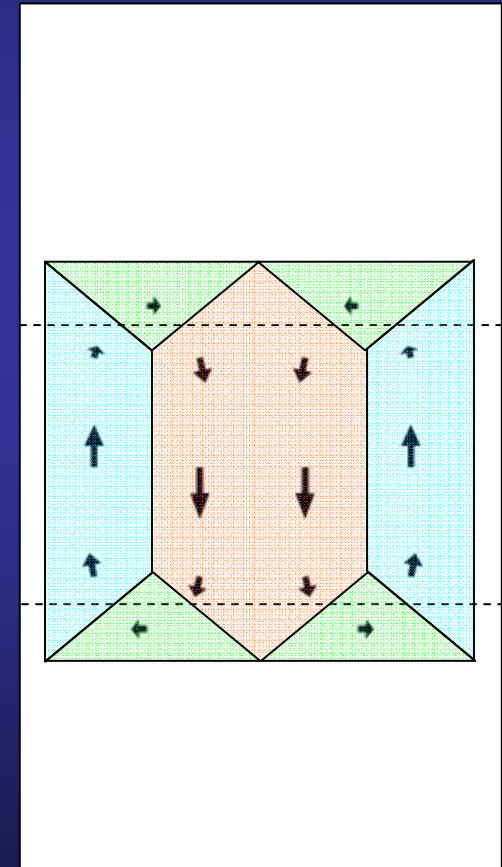
$N_x = 4$

BaO domain walls

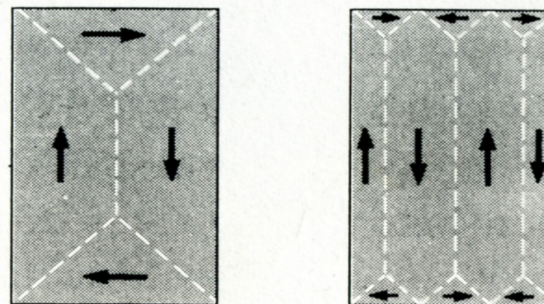


$N_x = 4$

BaO domain walls



Ferromagnetic domains

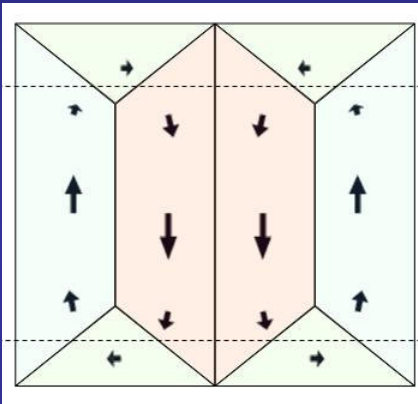


C. Kittel (1946)

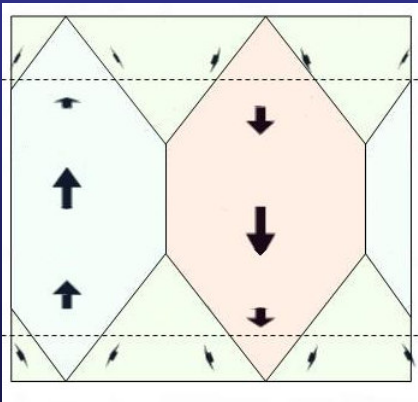
# Polydomain phases adopt the form of a “domain of closure”, common in ferromagnets

$N_x=4$

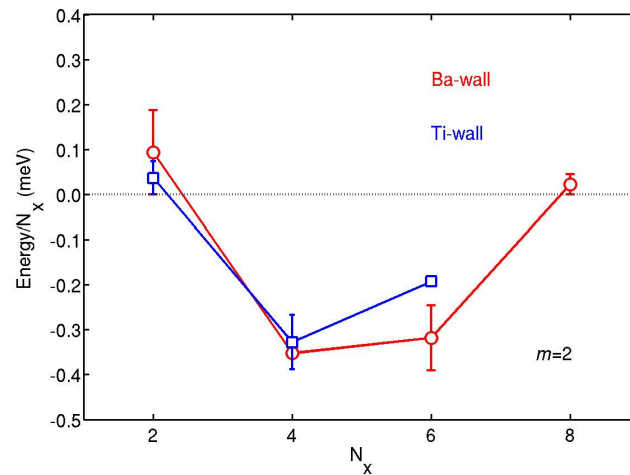
BaO wall



TiO<sub>2</sub> wall

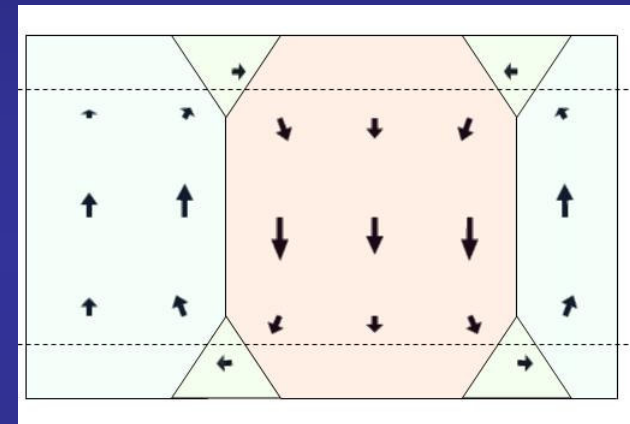


2-unit-cells thick BaTiO<sub>3</sub> layer

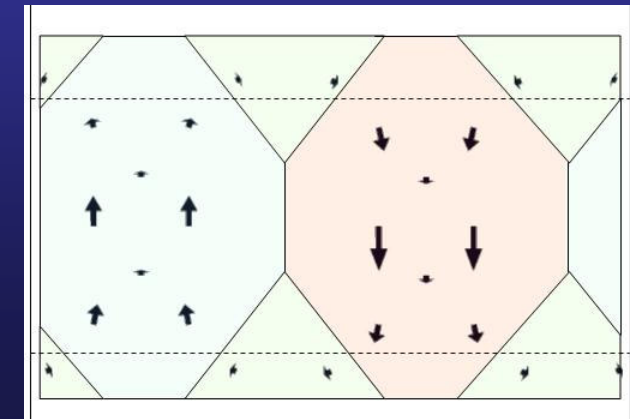


$N_x=6$

BaO wall



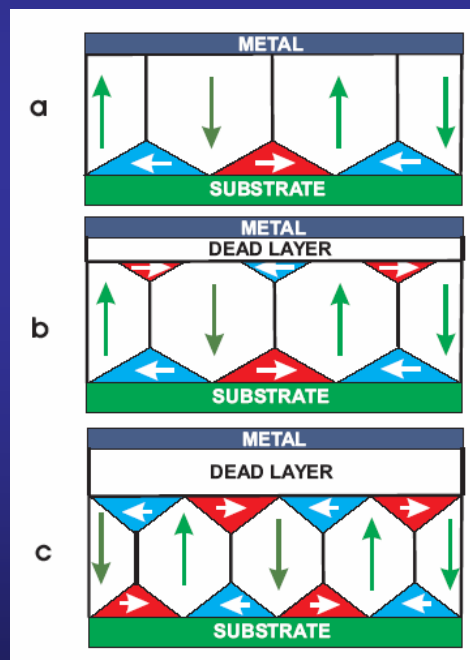
TiO<sub>2</sub> wall



# Domains of closure recently predicted using a model hamiltonian approach

48 Å thick  $\text{PbZr}_{0.4}\text{Ti}_{0.6}\text{O}_3$  thin films

sandwiched with a nongrounded metallic plate (top) and a non-conductive substrate (bottom)

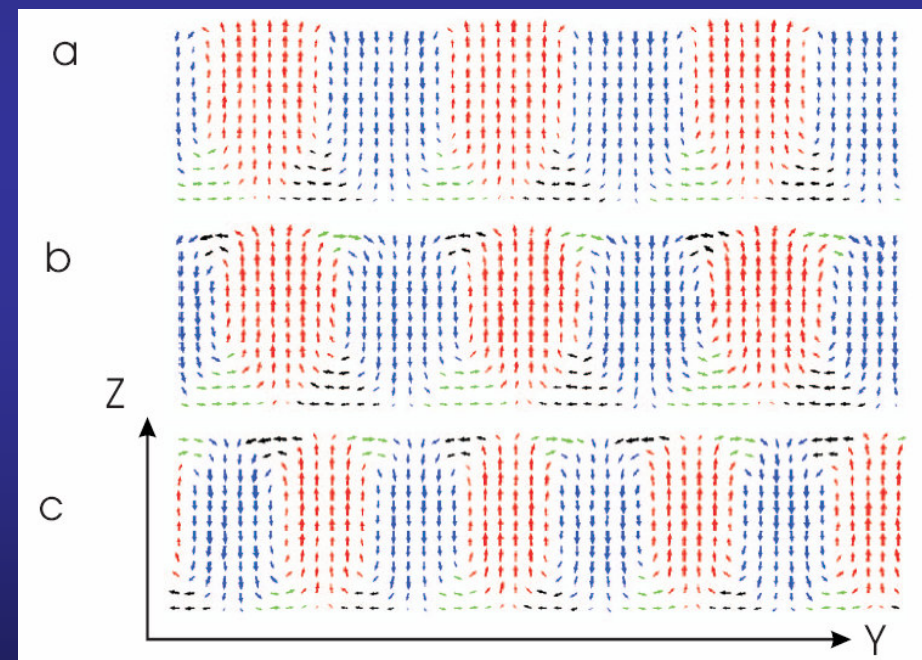


$d = 0$

$d = 0.3 a$

$d = 0.5 a$

Dead layer thickness

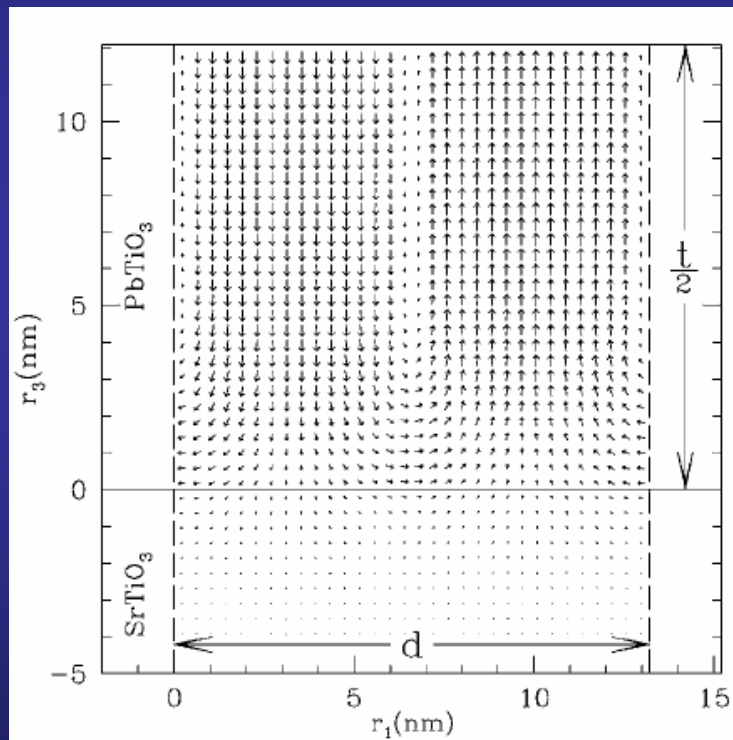


S. Prosandeev and L. Bellaiche, Phys. Rev. B 75, 172109 (2007)

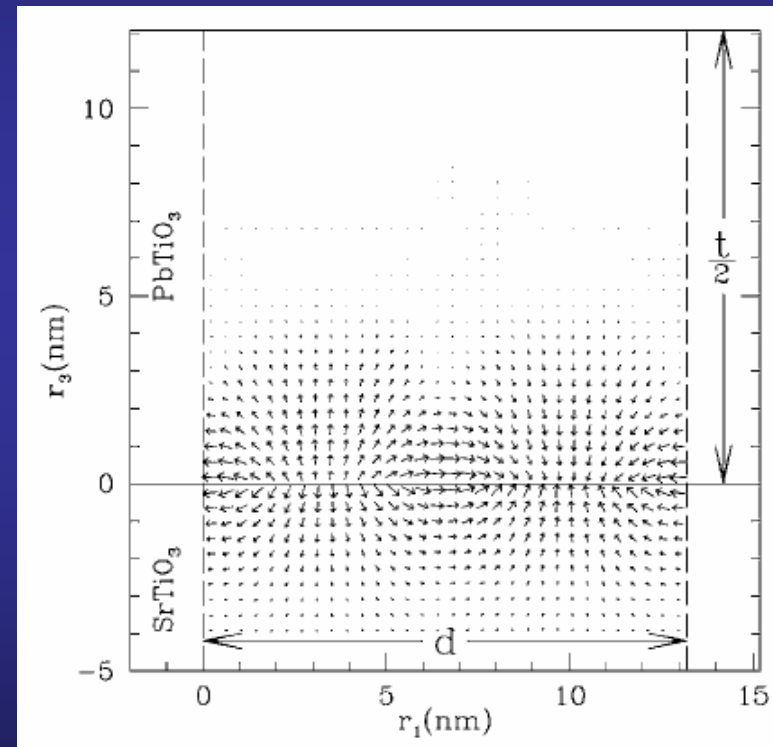
# Domains of closure recently predicted using a phenomenological thermodynamic potential

**242 Å thick  $\text{PbTiO}_3$  thin films**

sandwiched with a nonconducting  $\text{SrTiO}_3$  electrodes @ 700 K  
stripe period 132 Å



**Polarization distribution**

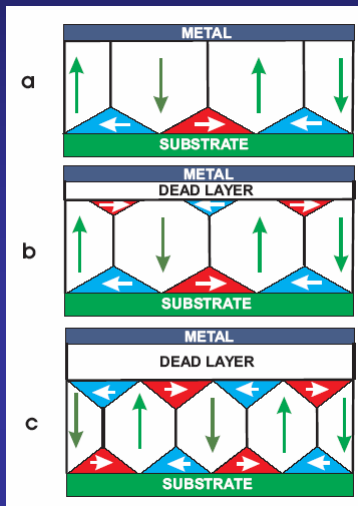


**Equilibrium field distribution**

G. B. Stephenson and K. R. Elder, J. Appl. Phys. 100, 051601 (2006)

# Full first-principles simulations: the domains of closure structure is more general than expected

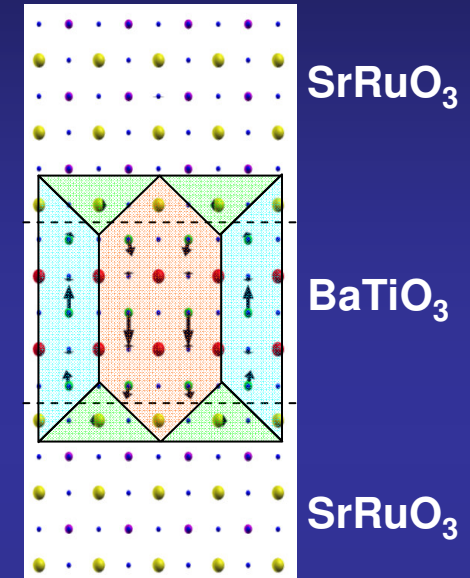
Domains of closure appear even with symmetric metallic electrode



S. Prosandeev and L. Bellaiche,  
Phys. Rev. B 75, 172109 (2007)

Case I:	Case II:	Case III:
$\text{SrTiO}_3$	Conductor	Vacuum
$\text{PbTiO}_3$	$\text{PbTiO}_3$	$\text{PbTiO}_3$
$\text{SrTiO}_3$	$\text{SrTiO}_3$	$\text{SrTiO}_3$

G. B. Stephenson and K. R. Elder,  
J. Appl. Phys. 100, 051601 (2006)



This work

## Domains of closure appear even in $\text{BaTiO}_3$ ferroelectric capacitors

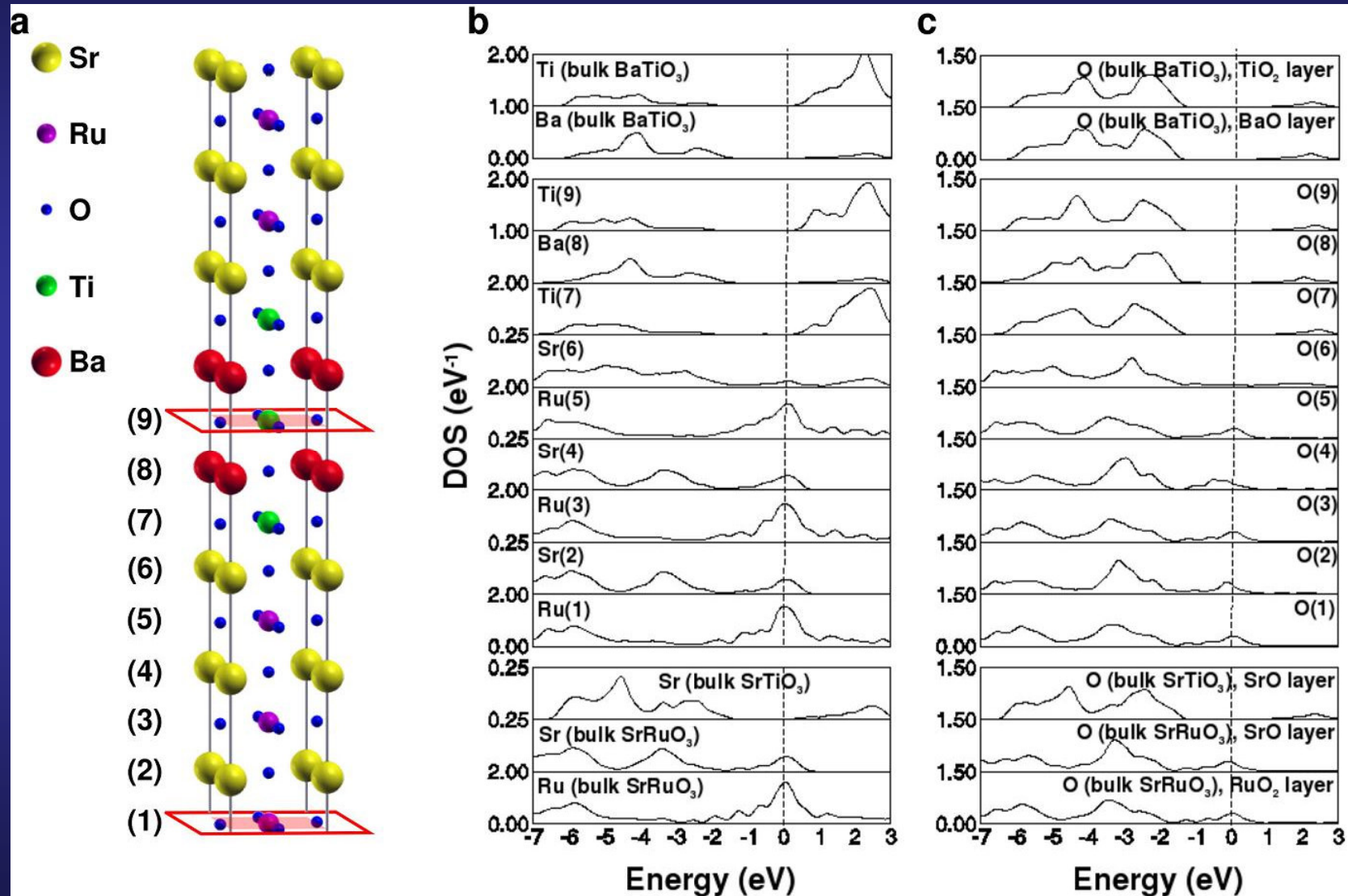
“ $\text{BaTiO}_3$  profoundly dislike significantly rotating and in-plane dipole”

“ $\text{BaTiO}_3$  with the PZT configuration is thermodynamically unstable because it directly transforms into 180 stripe domains after a couple of Monte Carlo sweeps”

B. -K. Lai et al., Phys. Rev. B 75, 085412 (2007)



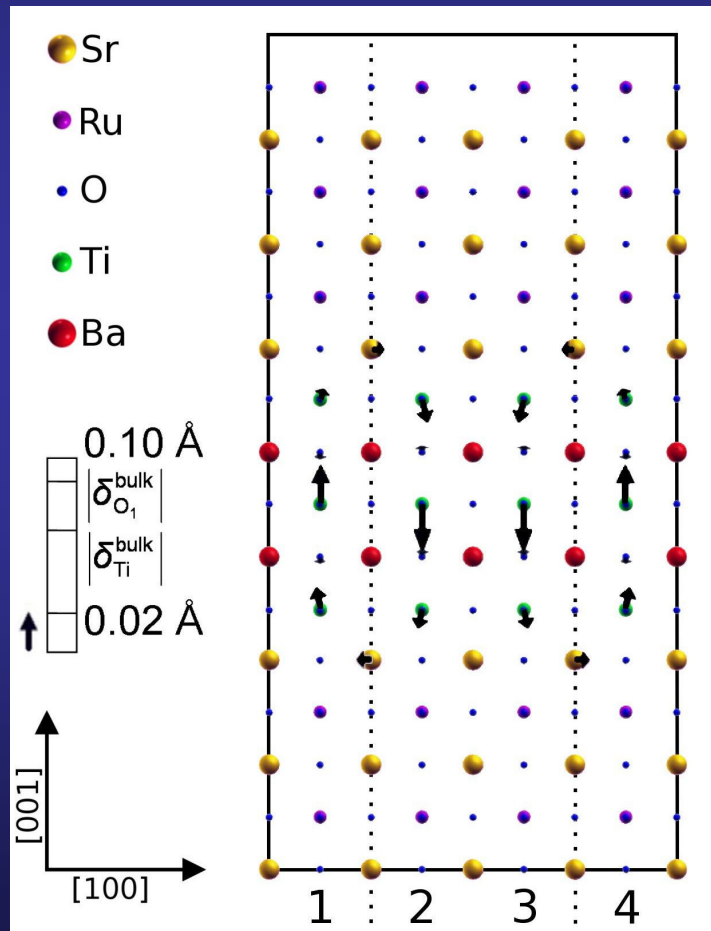
# SrO layer at the interface behaves more like SrTiO<sub>3</sub> than SrRuO<sub>3</sub> ⇒ highly polarizable



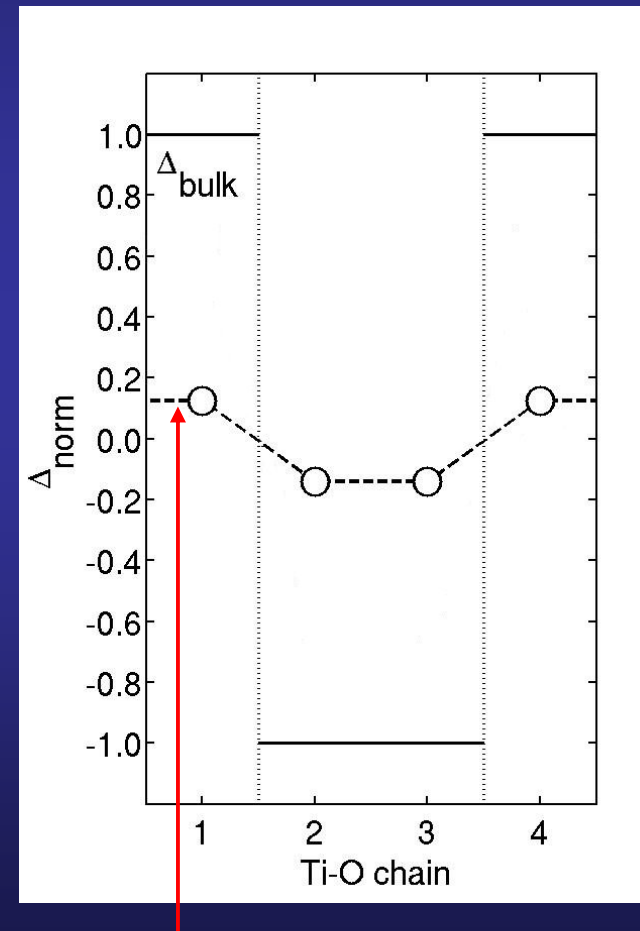
Projected Density of States in the reference paraelectric structure

# Resulting phases show in-plane displacements and small polarization

$N_x = 4$   
BaO domain walls



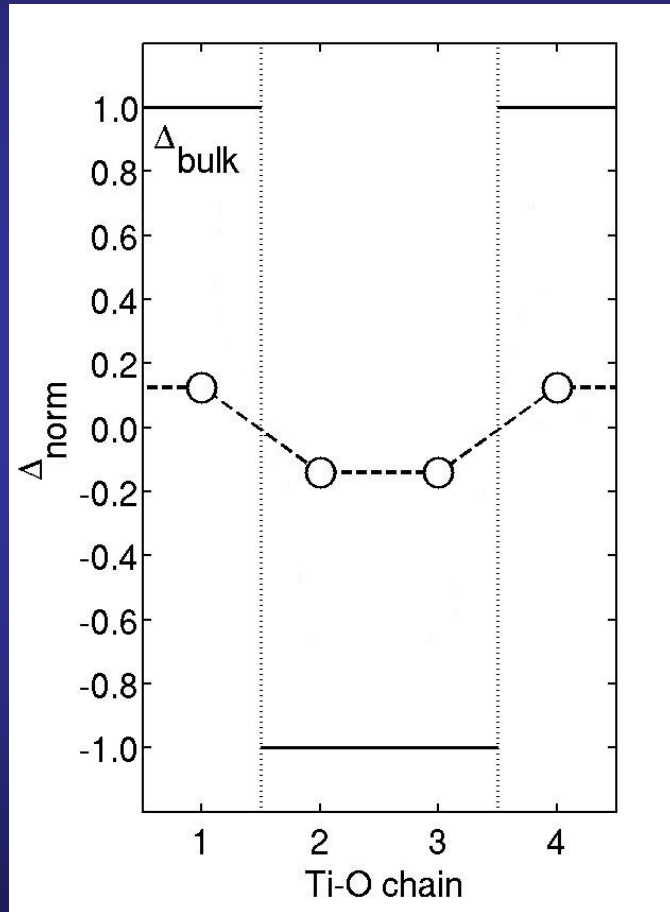
Small polarization inside the domains



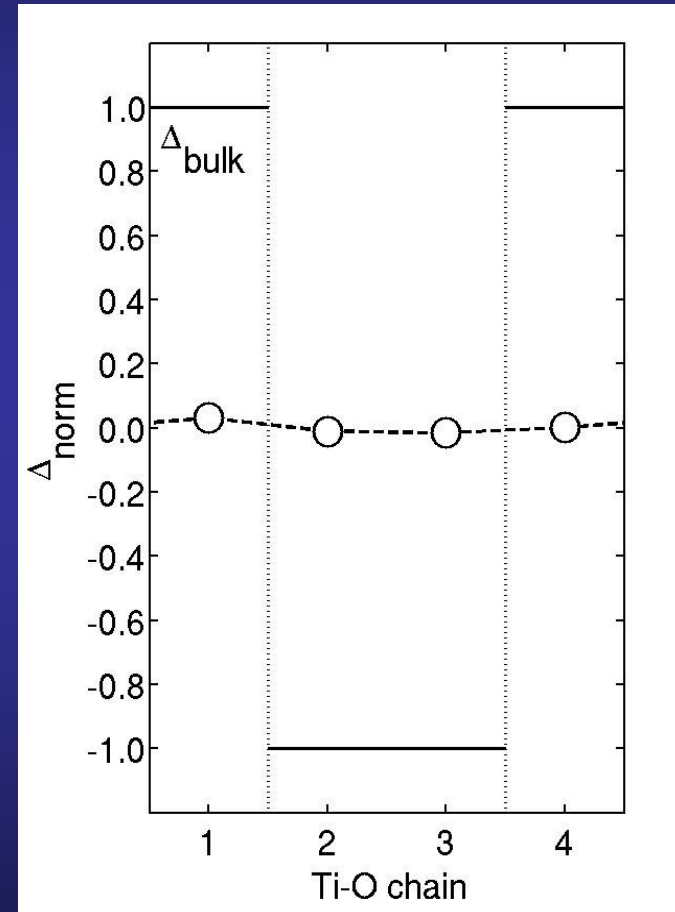
About 1/10 of bulk soft-mode polarization

# In-plane displacements are very important to stabilize the domains

In-plane displacements: ON

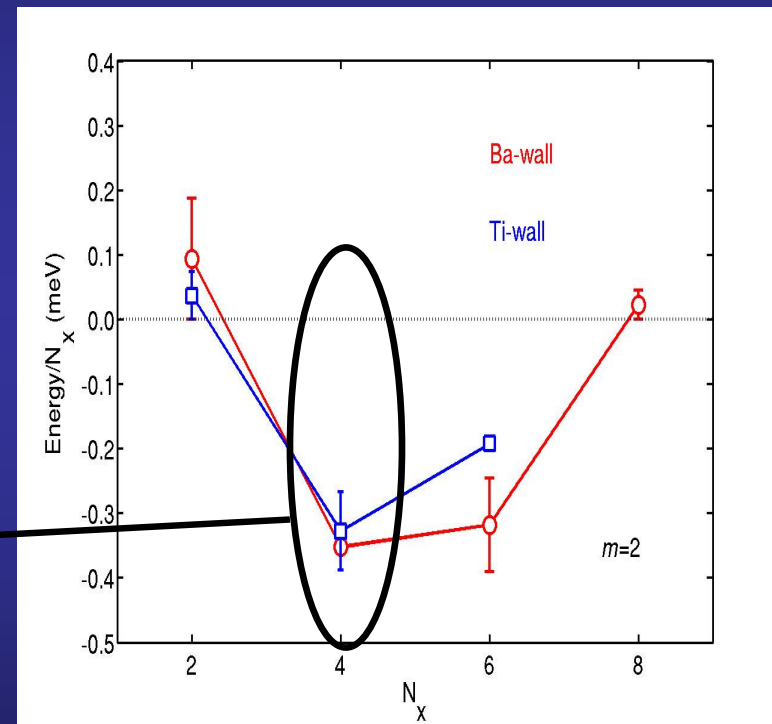
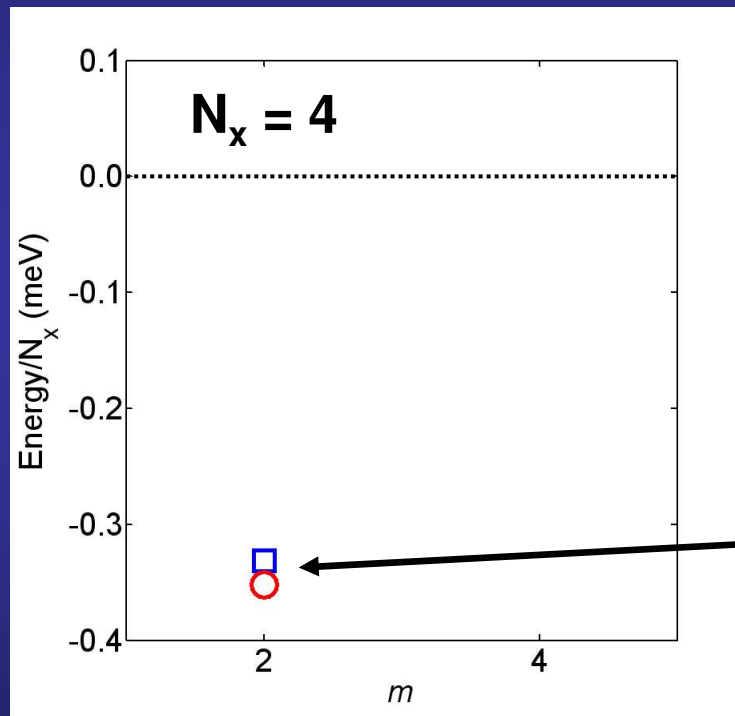


In-plane displacements: OFF

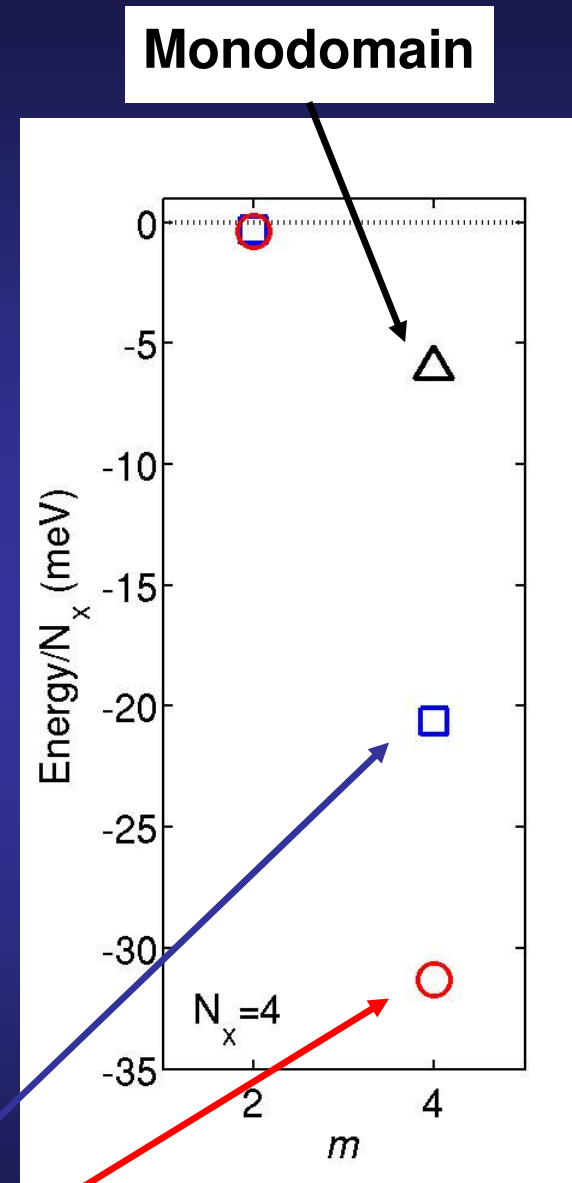
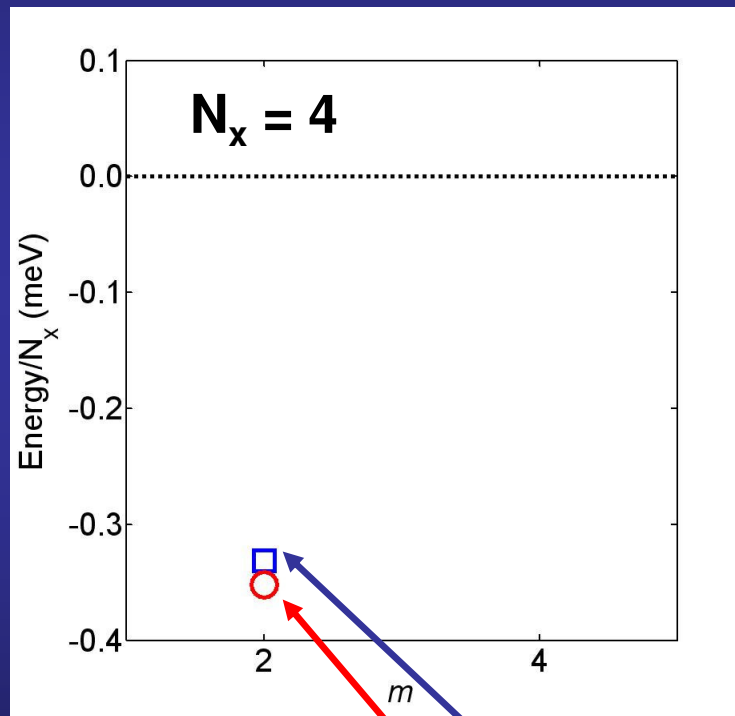


When in-plane coordinates are fixed, structure goes back to the paraelectric phase

# Relevant energy differences very small in the ultrathin $m = 2$ capacitors



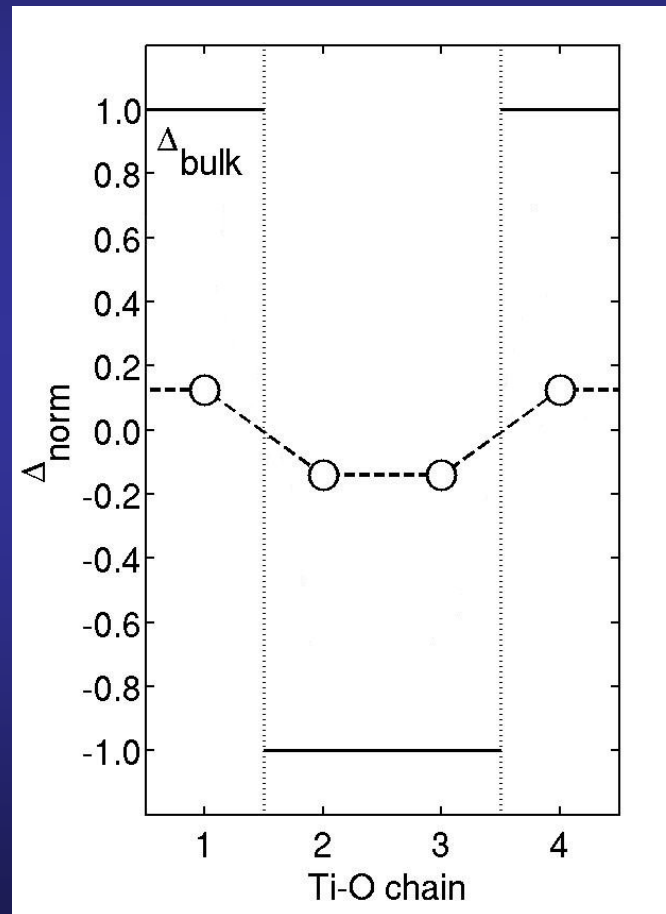
# Relevant energy differences increase with thickness



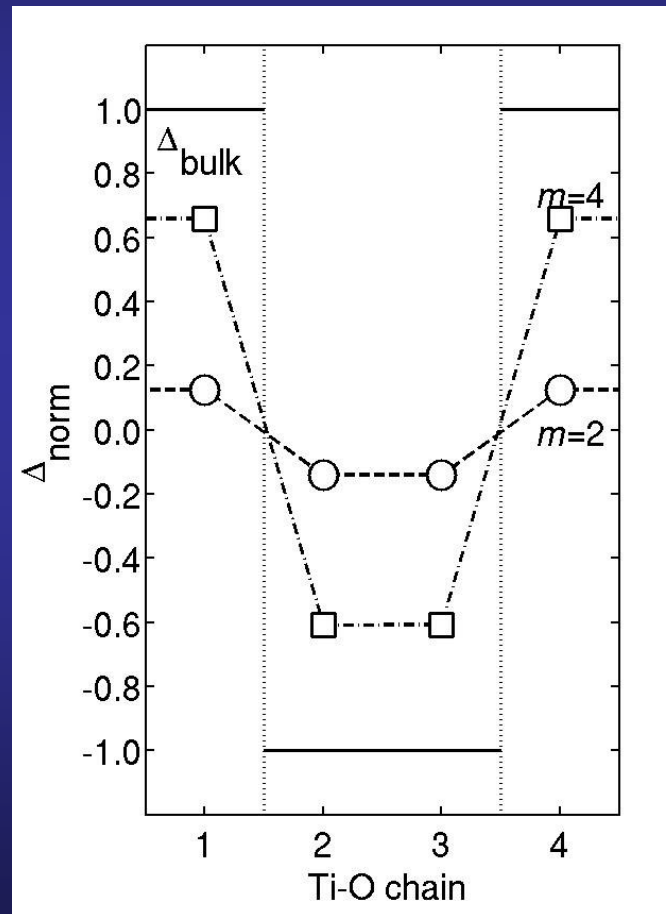
Ti-centered domains

Ba-centered domains

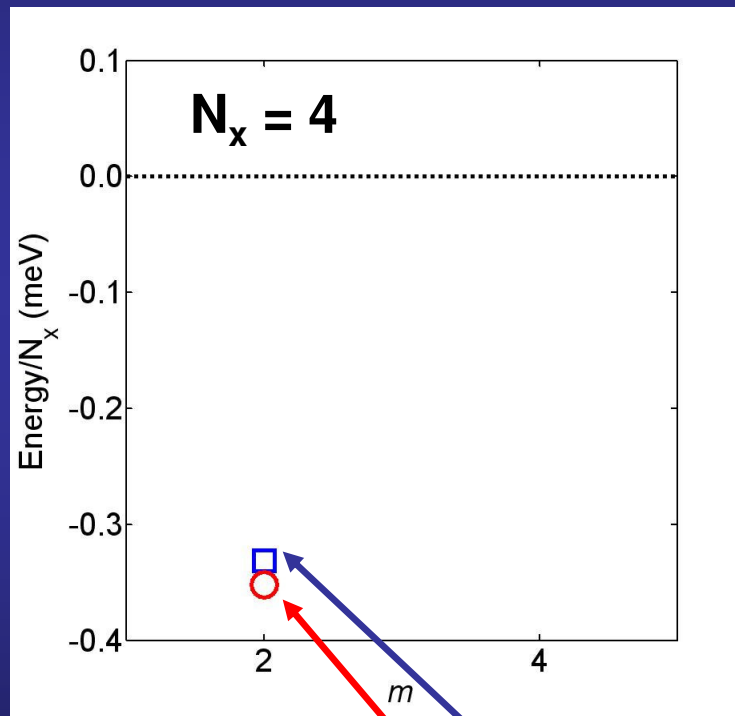
# Transition from vortices to standard 180° domains. 4-unit-cell thick layer, great increase in polarization



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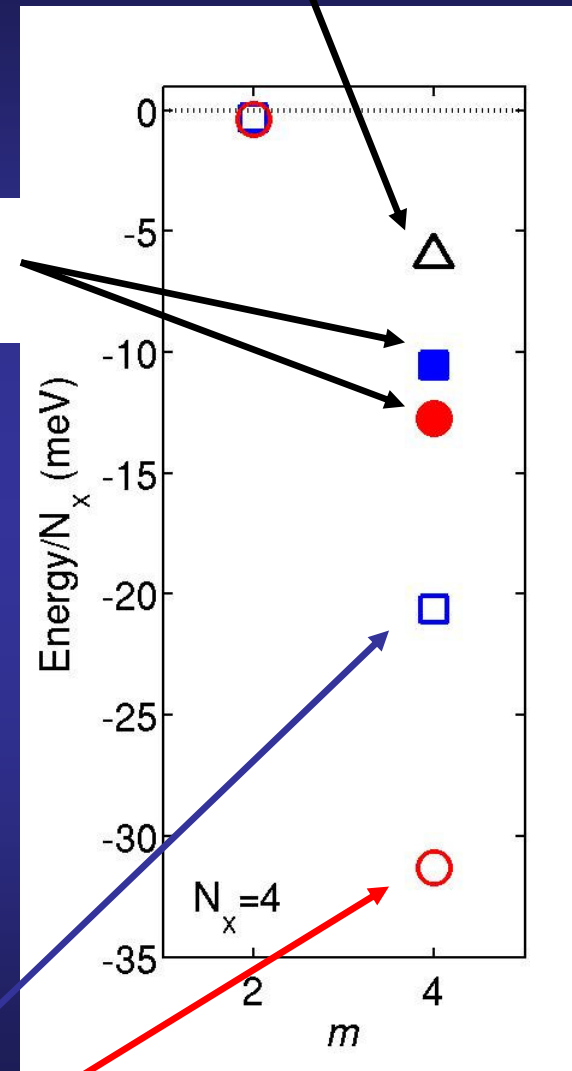


# In-plane displacements, contribute to stabilize domains



In-plane constraint

Monodomain



Ti-centered domains

Ba-centered domains

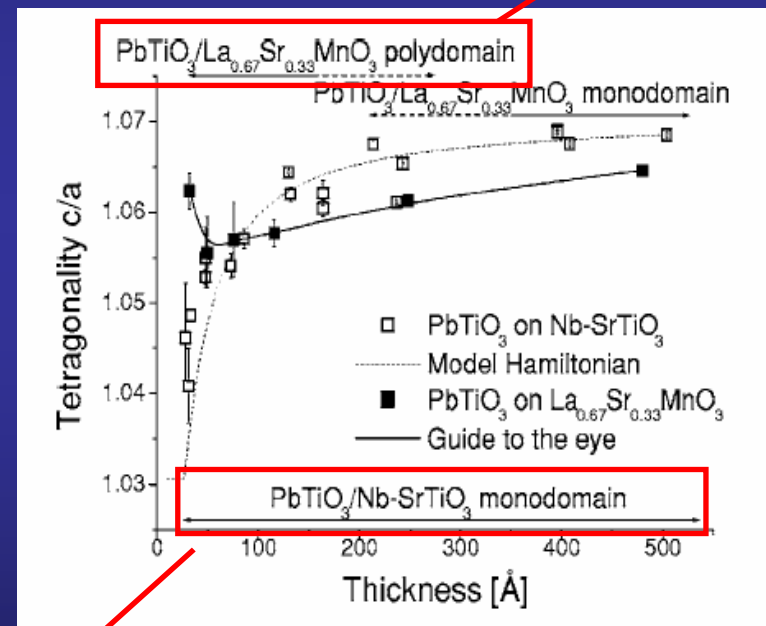


# Changing the electrode, the ground state of $\text{PbTiO}_3$ changes from monodomain to polydomain

APPLIED PHYSICS LETTERS 90, 052907 (2007)

Monodomain to polydomain transition in ferroelectric  $\text{PbTiO}_3$  thin films with  $\text{La}_{0.67}\text{Sr}_{0.33}\text{MnO}_3$  electrodes

Lichtensteiger, *et al.*



PRL 94, 047603 (2005)

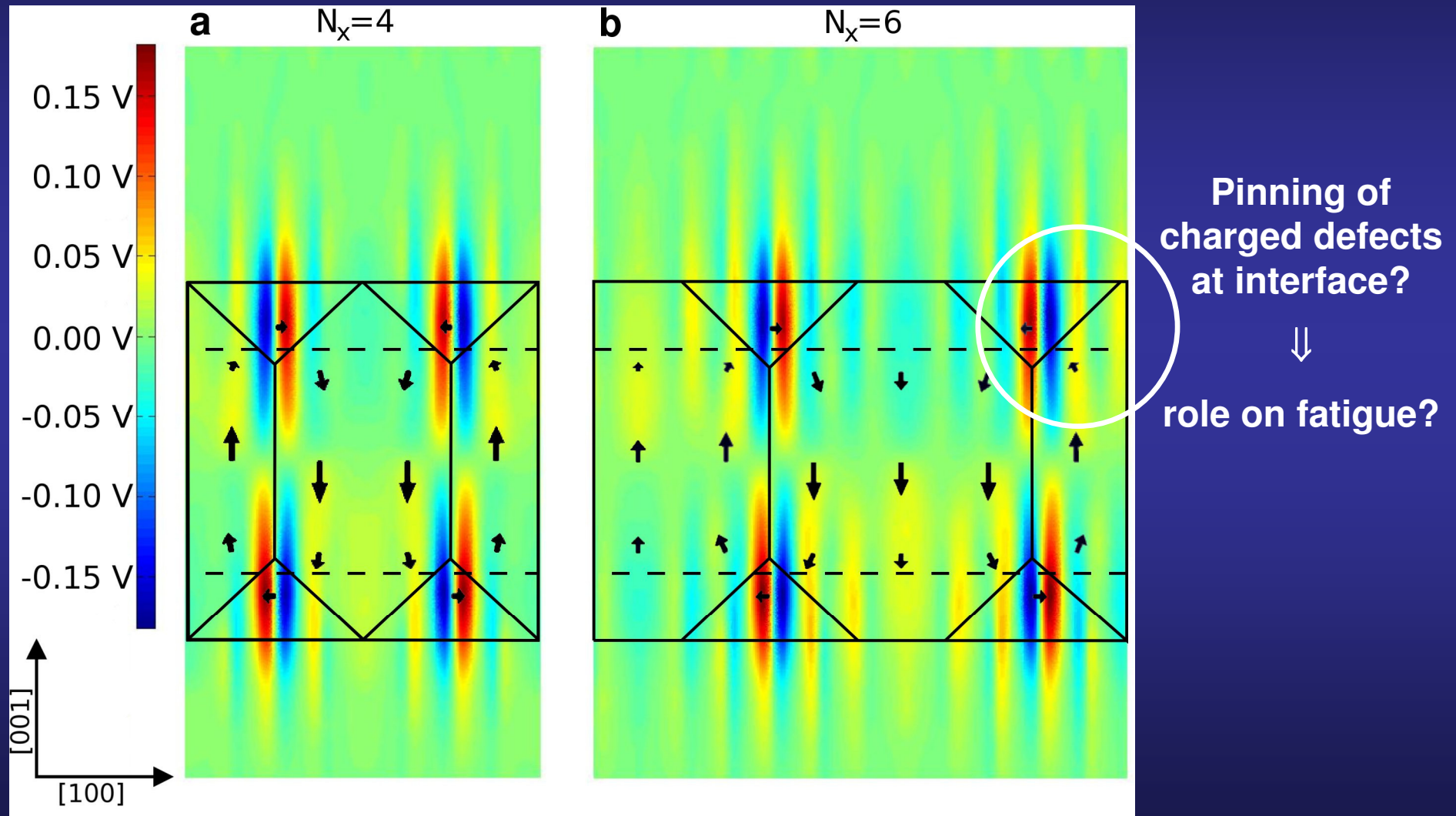
PHYSICAL REVIEW LETTERS

week ending  
4 FEBRUARY 2005

Ferroelectricity and Tetragonality in Ultrathin  $\text{PbTiO}_3$  Films

Lichtensteiger, Triscone, Junquera, Ghosez.

# Analysis of the electrostatic potential: large field in $x$ at the interface, residual depolarizing field in $z$



Two unit cells thick of  $\text{BaTiO}_3$

# Preliminary results on $\text{SrRuO}_3/\text{PbTiO}_3/\text{SrRuO}_3$ $m = 2, N_x = 6$ remain paraelectric

Good agreement with experiment

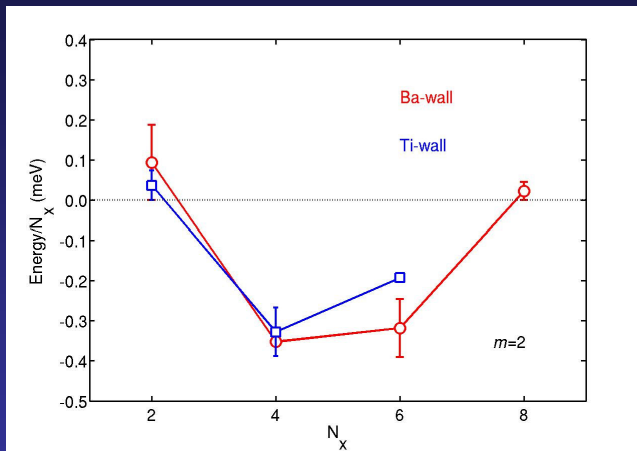
## Ferroelectricity in Ultrathin Perovskite Films

Dillon D. Fong,<sup>1</sup> G. Brian Stephenson,<sup>1\*</sup> Stephen K. Streiffer,<sup>1</sup>  
Jeffrey A. Eastman,<sup>1</sup> Orlando Auciello,<sup>1</sup> Paul H. Fuoss,<sup>1</sup>  
Carol Thompson<sup>2</sup>

At 1

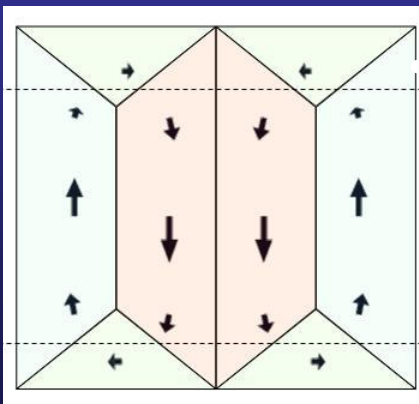
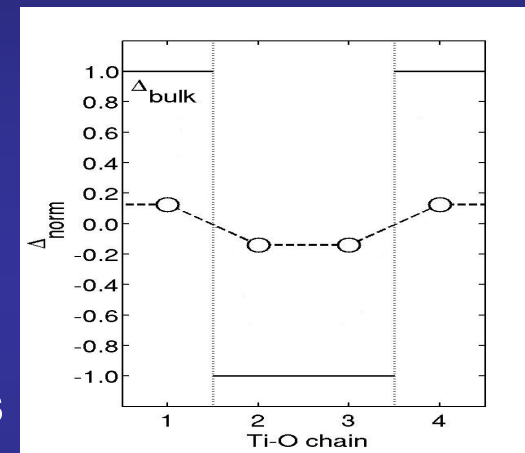
and 2 unit cells, no satellites are observed at any temperature, indicating that the samples remain in the paraelectric phase.

# Conclusions



- **Polydomain phases** in ultrathin FE films are stabilized below critical thickness in monodomain configurations.

- The chemical interaction through the interface is an essential factor since it affects the **in-plane mobility** of the atoms.



Polydomains phases have a structure: **Closure domains**

Slides available at: <http://personales.unican.es/junqueraj>

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