

T18.- Intercambiadores de Calor. Método de la Eficiencia

Las transparencias son el material de apoyo del profesor para impartir la clase. No son apuntes de la asignatura. Al alumno le pueden servir como guía para recopilar información (libros, ...) y elaborar sus propios apuntes

Departamento: Ingeniería Eléctrica y Energética
Area: Máquinas y Motores Térmicos

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1

**XVIII.- INTERCAMBIADORES DE CALOR
MÉTODO DE LA EFICIENCIA**

XVIII.1.- EFICACIA DE LOS INTERCAMBIADORES DE CALOR, ε (I)

Se conoce la descripción del intercambiador y las T^{as} de entrada, desconociendo las de salida

ε compara transferencia térmica en el fluido frío

$$\varepsilon = \frac{\text{Velocidad real de transferencia de calor en un intercambiador determinado}}{\text{Velocidad máxima posible de transferencia de calor}}$$

$Q_{m\acute{a}x}$ intercambiador en contracorriente, A infinita

$$Q = C_C (T_{C1} - T_{C2}) = C_F (T_{F2} - T_{F1})$$

Supuesto sin pérdidas térmicas:

$$\text{Si } C_C < C_F \Rightarrow \Delta T_C > \Delta T_F \Rightarrow T_{C2\text{mín}} = T_{F1} \text{ y } Q_{m\acute{a}x} = C_C (T_{C1} - T_{F1})$$

$$\text{Si } C_F < C_C \Rightarrow \Delta T_F > \Delta T_C \Rightarrow T_{F2\text{m\acute{a}x}} = T_{C1} \text{ y } Q_{m\acute{a}x} = C_F (T_{C1} - T_{F1})$$

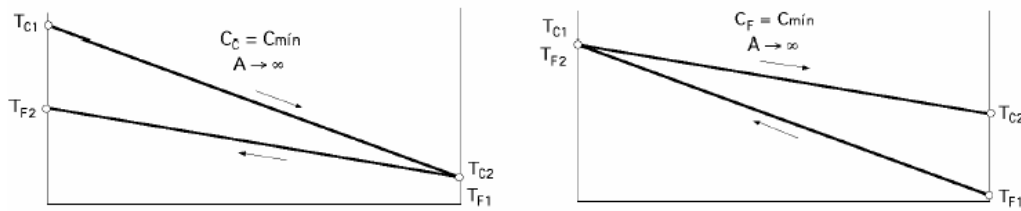
En cualquier caso:

$$Q_{m\acute{a}x} = C_{m\acute{i}n} (T_{C1} - T_{F1})$$

2

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.1.- EFICACIA DE LOS INTERCAMBIADORES DE CALOR, ϵ (II)



$$\epsilon = \frac{Q}{Q_{\text{máx}}} = \frac{Q}{C_{\text{mín}} (T_{C1} - T_{F1})} = \frac{C_F (T_{F2} - T_{F1})}{C_{\text{mín}} (T_{C1} - T_{F1})} = \frac{C_C (T_{C1} - T_{C2})}{C_{\text{mín}} (T_{C1} - T_{F1})}$$

$$\boxed{Q = \epsilon C_{\text{mín}} (T_{C1} - T_{F1})} = C_F (T_{F2} - T_{F1}) = C_C (T_{C1} - T_{C2})$$

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.2.- EFICACIA, CASO FLUJOS PARALELOS EN EQUICORRIENTE (I)

$$Q = \epsilon C_{\text{mín}} (T_{C1} - T_{F1}) = UA \frac{\Delta T_2 - \Delta T_1}{\ln \frac{\Delta T_2}{\Delta T_1}} = \left. \begin{array}{l} \Delta T_2 = T_{C1} - T_{F1} \\ \Delta T_1 = T_{C2} - T_{F2} \end{array} \right| = UA \frac{(T_{C1} - T_{F1}) - (T_{C2} - T_{F2})}{\ln \frac{T_{C1} - T_{F1}}{T_{C2} - T_{F2}}}$$

$$\boxed{\ln \frac{T_{C1} - T_{F1}}{T_{C2} - T_{F2}} = UA \frac{(T_{C1} - T_{C2}) - (T_{F1} - T_{F2})}{\epsilon C_{\text{mín}} (T_{C1} - T_{F1})}} \quad (***) = (**)$$

$$\begin{aligned} (***) \quad UA \frac{(T_{C1} - T_{C2}) - (T_{F1} - T_{F2})}{\epsilon C_{\text{mín}} (T_{C1} - T_{F1})} &= \epsilon = \frac{C_F (T_{F2} - T_{F1})}{C_{\text{mín}} (T_{C1} - T_{F1})} = \frac{C_C (T_{C1} - T_{C2})}{C_{\text{mín}} (T_{C1} - T_{F1})} \\ &= \frac{UA}{\epsilon C_{\text{mín}}} \left(\frac{T_{C1} - T_{C2}}{T_{C1} - T_{F1}} + \frac{T_{F2} - T_{F1}}{T_{C1} - T_{F1}} \right) = \frac{T_{F2} - T_{F1}}{T_{C1} - T_{F1}} = \frac{\epsilon C_{\text{mín}}}{C_F} \\ &= \frac{UA}{\epsilon C_{\text{mín}}} \left(\frac{\epsilon C_{\text{mín}}}{C_C} + \frac{\epsilon C_{\text{mín}}}{C_F} \right) = \frac{T_{C1} - T_{C2}}{T_{C1} - T_{F1}} = \frac{\epsilon C_{\text{mín}}}{C_C} \\ &= UA \left(\frac{1}{C_C} + \frac{1}{C_F} \right) (***) \end{aligned}$$

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.2.- EFICACIA, CASO FLUJOS PARALELOS EN EQUICORRIENTE (II)

(**)

$$\ln \frac{T_{C1} - T_{F1}}{T_{C2} - T_{F2}} = \left\{ \begin{array}{l} \varepsilon C_{\min} (T_{C1} - T_{F1}) = C_C (T_{C1} - T_{C2}) \rightarrow T_{C2} = T_{C1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_C} \\ \varepsilon C_{\min} (T_{C1} - T_{F1}) = C_F (T_{F2} - T_{F1}) \rightarrow T_{F2} = T_{F1} + (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_F} \end{array} \right.$$

$$= \ln \frac{T_{C1} - T_{F1}}{T_{C1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_C} - T_{F1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_F}} =$$

$$= \ln \frac{T_{C1} - T_{F1}}{T_{C1} (1 - \frac{\varepsilon C_{\min}}{C_C} - \frac{\varepsilon C_{\min}}{C_F}) - T_{F1} (1 - \frac{\varepsilon C_{\min}}{C_C} - \frac{\varepsilon C_{\min}}{C_F})} =$$

$$= \ln \frac{1}{1 - \varepsilon C_{\min} (\frac{1}{C_C} + \frac{1}{C_F})} = - \ln \{ 1 - \varepsilon C_{\min} (\frac{1}{C_C} + \frac{1}{C_F}) \} \quad (**)$$

5

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.2.- EFICACIA, CASO FLUJOS PARALELOS EN EQUICORRIENTE (III)

$$\ln \frac{T_{C1} - T_{F1}}{T_{C2} - T_{F2}} = UA \frac{(T_{C1} - T_{C2}) - (T_{F1} - T_{F2})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} \quad (**) = (**)$$

$$\left\{ \begin{array}{l} UA \frac{(T_{C1} - T_{C2}) - (T_{F1} - T_{F2})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} = UA (\frac{1}{C_C} + \frac{1}{C_F}) \quad (**) \\ \ln \frac{T_{C1} - T_{F1}}{T_{C2} - T_{F2}} = - \ln \{ 1 - \varepsilon C_{\min} (\frac{1}{C_C} + \frac{1}{C_F}) \} \quad (**) \end{array} \right.$$

$$- \ln \{ 1 - \varepsilon C_{\min} (\frac{1}{C_C} + \frac{1}{C_F}) \} = UA (\frac{1}{C_C} + \frac{1}{C_F}) \quad \frac{UA}{C_{\min}} = NTU$$

$$1 - \varepsilon (\frac{C_{\min}}{C_C} + \frac{C_{\min}}{C_F}) = e^{-UA (\frac{1}{C_C} + \frac{1}{C_F})}$$

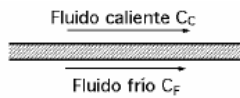
$$\varepsilon = \frac{1 - e^{-UA (\frac{1}{C_C} + \frac{1}{C_F})}}{\frac{C_{\min}}{C_C} + \frac{C_{\min}}{C_F}} = \frac{1 - e^{-\frac{UA}{C_{\min}} (\frac{C_{\min}}{C_{\max}} + 1)}}{\frac{C_{\min}}{C_{\max}} + 1}$$

$$\varepsilon = \frac{1 - e^{-NTU (\frac{C_{\min}}{C_{\max}} + 1)}}{\frac{C_{\min}}{C_{\max}} + 1}$$

6

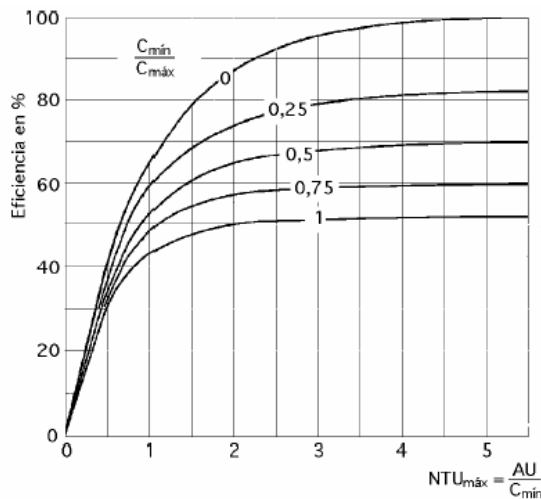
XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.2.- EFICACIA, CASO FLUJOS PARALELOS EN EQUICORRIENTE (IV)



$$\frac{UA}{C_{\min}} = NTU$$

$$\varepsilon = \frac{1 - e^{-NTU \left(\frac{C_{\min}}{C_{\max}} + 1 \right)}}{\frac{C_{\min}}{C_{\max}} + 1}$$



$$\left. \begin{array}{l} A \rightarrow \infty \\ C_{\min} \ll C_{\max} \end{array} \right\} \Rightarrow T_{C2} = T_{F1} \text{ o } T_{F2} = T_{C1} \Rightarrow \varepsilon \approx 1$$

Tª de un fluido cte: condensación, evaporación, sist. calef., ...

$$\left. \begin{array}{l} A \rightarrow \infty \\ C_{\min} = C_{\max} \end{array} \right\} \Rightarrow T_{C2} = T_{F2} = \frac{(T_{C1} + T_{F1})}{2} \Rightarrow \varepsilon = 0,5$$

7

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.3.- EFICACIA, CASO FLUJOS PARALELOS EN CONTRACORRIENTE (I)

$$Q = \varepsilon C_{\min} (T_{C1} - T_{F1}) = UA \frac{\Delta T_2 - \Delta T_1}{\ln \frac{\Delta T_2}{\Delta T_1}} = \left| \begin{array}{l} \Delta T_2 = T_{C1} - T_{F2} \\ \Delta T_1 = T_{C2} - T_{F1} \end{array} \right| = UA \frac{(T_{C1} - T_{F2}) - (T_{C2} - T_{F1})}{\ln \frac{T_{C1} - T_{F2}}{T_{C2} - T_{F1}}}$$

$$\ln \frac{T_{C1} - T_{F2}}{T_{C2} - T_{F1}} = UA \frac{(T_{C1} - T_{C2}) - (T_{F2} - T_{F1})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} \quad (***) = (**)$$

$$\begin{aligned} (***) \quad UA \frac{(T_{C1} - T_{C2}) - (T_{F2} - T_{F1})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} &= \varepsilon = \frac{C_F (T_{F2} - T_{F1})}{C_{\min} (T_{C1} - T_{F1})} = \frac{C_C (T_{C1} - T_{C2})}{C_{\min} (T_{C1} - T_{F1})} \\ &= \frac{UA}{\varepsilon C_{\min}} \left(\frac{T_{C1} - T_{C2}}{T_{C1} - T_{F1}} - \frac{T_{F2} - T_{F1}}{T_{C1} - T_{F1}} \right) = \frac{T_{F2} - T_{F1}}{T_{C1} - T_{F1}} = \frac{\varepsilon C_{\min}}{C_F} \\ &= \frac{UA}{\varepsilon C_{\min}} \left(\frac{\varepsilon C_{\min}}{C_C} - \frac{\varepsilon C_{\min}}{C_F} \right) = \frac{T_{C1} - T_{C2}}{T_{C1} - T_{F1}} = \frac{\varepsilon C_{\min}}{C_C} \\ &= UA \left(\frac{1}{C_C} - \frac{1}{C_F} \right) \quad (***) \end{aligned}$$

8

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.3.- EFICACIA, CASO FLUJOS PARALELOS EN CONTRACORRIENTE (II)

(**)

$$\ln \frac{T_{C1} - T_{F2}}{T_{C2} - T_{F1}} = \left\{ \begin{array}{l} \varepsilon C_{\min} (T_{C1} - T_{F1}) = C_C (T_{C1} - T_{C2}) \rightarrow T_{C2} = T_{C1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_C} \\ \varepsilon C_{\min} (T_{C1} - T_{F1}) = C_F (T_{F2} - T_{F1}) \rightarrow T_{F2} = T_{F1} + (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_F} \end{array} \right.$$

$$= \ln \frac{T_{C1} - T_{F1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_C}}{T_{C1} - (T_{C1} - T_{F1}) \frac{\varepsilon C_{\min}}{C_C} - T_{F1}} = \ln \frac{(T_{C1} - T_{F1}) \left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)}{(T_{C1} - T_{F1}) \left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)} =$$

$$= \ln \frac{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)}{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)} \quad (**)$$

9

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.3.- EFICACIA, CASO FLUJOS PARALELOS EN CONTRACORRIENTE (III)

$$\ln \frac{T_{C1} - T_{F2}}{T_{C2} - T_{F1}} = UA \frac{(T_{C1} - T_{C2}) - (T_{F2} - T_{F1})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} \quad (**) = (**)$$

$$UA \frac{(T_{C1} - T_{C2}) - (T_{F2} - T_{F1})}{\varepsilon C_{\min} (T_{C1} - T_{F1})} = UA \left(\frac{1}{C_C} - \frac{1}{C_F} \right) \quad (**)$$

$$\ln \frac{T_{C1} - T_{F2}}{T_{C2} - T_{F1}} = \ln \frac{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)}{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)} \quad (**)$$

$$\ln \frac{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)}{\left(1 - \frac{\varepsilon C_{\min}}{C_C}\right)} = UA \left(\frac{1}{C_C} - \frac{1}{C_F} \right)$$

$$\frac{1 - \frac{\varepsilon C_{\min}}{C_C}}{1 - \frac{\varepsilon C_{\min}}{C_C}} = e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F} \right)} \rightarrow 1 - \frac{\varepsilon C_{\min}}{C_C} = \left(1 - \frac{\varepsilon C_{\min}}{C_C}\right) e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F} \right)}$$

10

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.3.- EFICACIA, CASO FLUJOS PARALELOS EN CONTRACORRIENTE (IV)

$$\begin{aligned} \rightarrow 1 - \frac{\varepsilon C_{\min}}{C_F} &= \left(1 - \frac{\varepsilon C_{\min}}{C_C}\right) e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} \\ 1 - \frac{\varepsilon C_{\min}}{C_F} &= e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} - \frac{\varepsilon C_{\min}}{C_C} e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} \\ 1 - e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} &= \frac{\varepsilon C_{\min}}{C_F} - \frac{\varepsilon C_{\min}}{C_C} e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} \\ 1 - e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} &= \varepsilon \left(\frac{C_{\min}}{C_F} - \frac{C_{\min}}{C_C} e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} \right) \end{aligned}$$

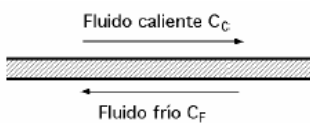
$$\varepsilon = \frac{1 - e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)}}{C_{\min} \left\{ \frac{1}{C_F} - \frac{1}{C_C} e^{UA \left(\frac{1}{C_C} - \frac{1}{C_F}\right)} \right\}}$$

$$\varepsilon = \frac{1 - e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1\right)}}{1 - \frac{C_{\min}}{C_{\max}} e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1\right)}}$$

11

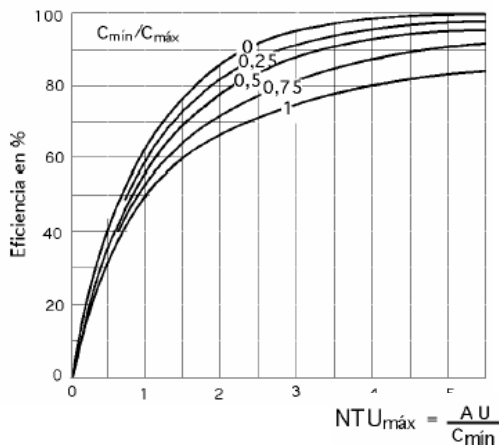
XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.3.- EFICACIA, CASO FLUJOS PARALELOS EN CONTRACORRIENTE (V)



$$\frac{UA}{C_{\min}} = NTU$$

$$\varepsilon = \frac{1 - e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1\right)}}{1 - \frac{C_{\min}}{C_{\max}} e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1\right)}}$$



$$\rightarrow A \rightarrow \infty \Rightarrow T_{C2} = T_{F1} \text{ o } T_{F2} = T_{C1} \Rightarrow \varepsilon \approx 1$$

12

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.4.- CONSIDERACIONES

Equicorriente

$$\varepsilon = \frac{1 - e^{-NTU \left(\frac{C_{\min}}{C_{\max}} + 1 \right)}}{\frac{C_{\min}}{C_{\max}} + 1}$$

Contracorriente

$$\varepsilon = \frac{1 - e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1 \right)}}{1 - \frac{C_{\min}}{C_{\max}} e^{-NTU \left(\frac{C_{\min}}{C_{\max}} - 1 \right)}}$$

Condensación o evaporación $\Rightarrow C_{\min} / C_{\max} = 0$

Tanto en equi como en contracorriente $\Rightarrow \varepsilon = 1 - e^{-NTU}$

Flujo equilibrado ($C_{\min} = C_{\max}$)

Equicorriente $\varepsilon = \frac{1 - e^{-2 NTU}}{2}$

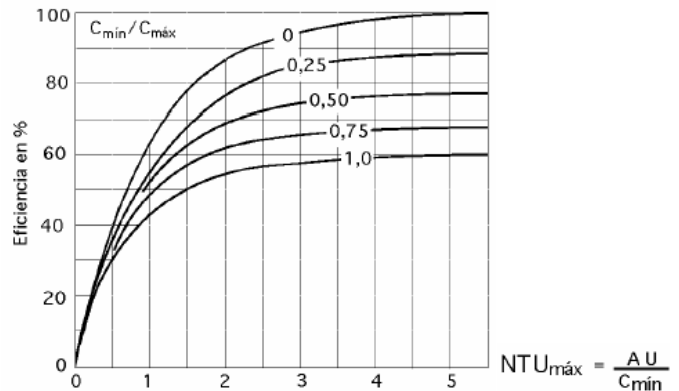
Contracorriente $\varepsilon = \frac{NTU}{1 + NTU}$

13

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.5.- OTRAS CONFIGURACIONES DE INTERCAMBIADORES

Un paso por carcasa y dos o múltiplo de dos pasos de tubo



$$NTU = - \frac{1}{\sqrt{1 + \left(\frac{C_{\min}}{C_{\max}} \right)^2}} \ln \frac{E - 1}{E + 1}$$

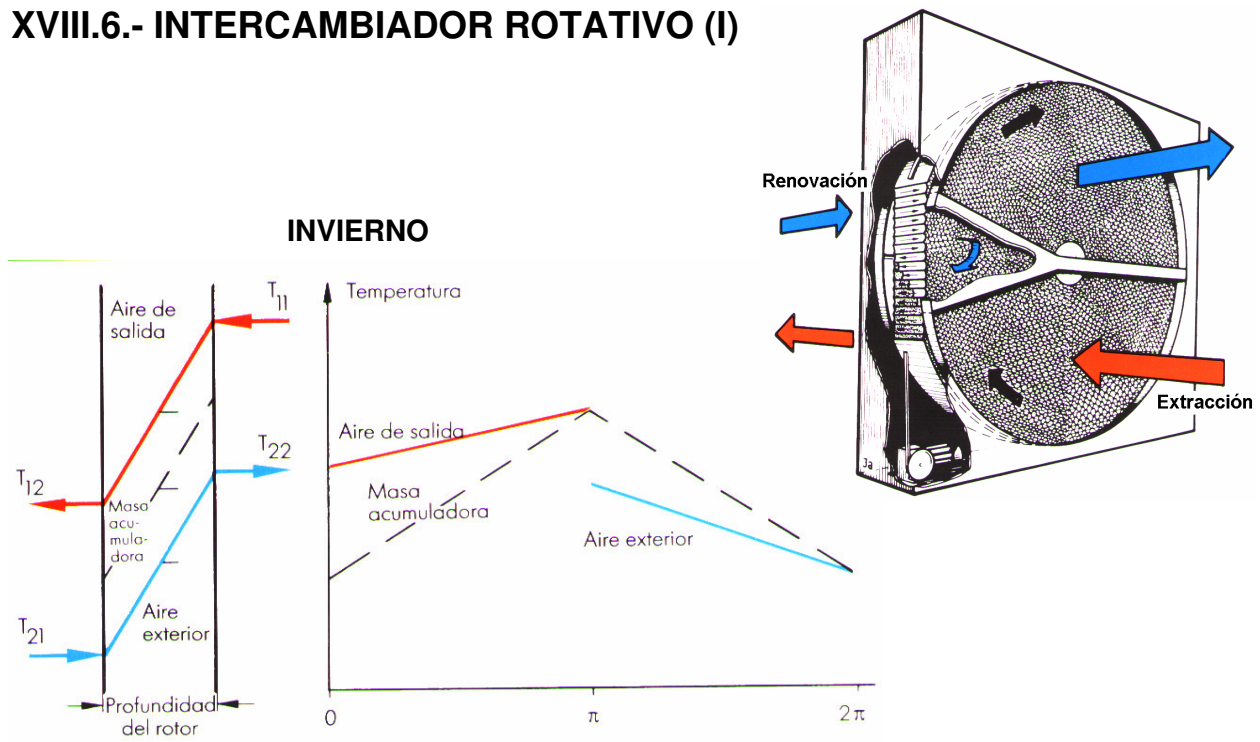
$$E = \frac{\frac{2}{\varepsilon} - \left(1 + \frac{C_{\min}}{C_{\max}} \right)}{\sqrt{1 + \left(\frac{C_{\min}}{C_{\max}} \right)^2}}$$

$$\varepsilon = \varepsilon_1 = 2 \left\{ 1 + \frac{C_{\min}}{C_{\max}} + \frac{1 + e^{-NTU \sqrt{1 + \left(\frac{C_{\min}}{C_{\max}} \right)^2}}}{1 - e^{-NTU \sqrt{1 + \left(\frac{C_{\min}}{C_{\max}} \right)^2}}} \sqrt{1 + \left(\frac{C_{\min}}{C_{\max}} \right)^2} \right\}$$

14

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.6.- INTERCAMBIADOR ROTATIVO (I)



15

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

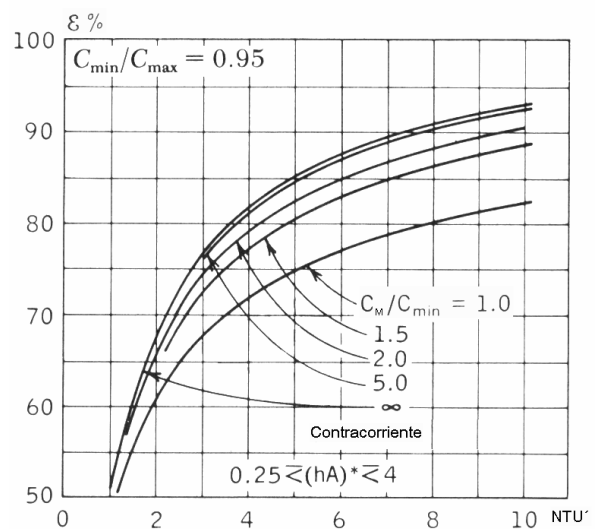
XVIII.6.- INTERCAMBIADOR ROTATIVO (II)

$$\frac{1}{UA} = \frac{1}{h_C A} + \frac{1}{h_F A} \implies UA = \frac{hA}{2}$$

$$C_M = N M_M c_{pM}, \quad \text{siendo } N \text{ el número de rpm}$$

$$\varepsilon = \varepsilon_{CC} \left[1 - \frac{1}{9 (C_M / C_{min})^{1,93}} \right]$$

siendo ε_{CC} la eficacia de un intercambiador en contracorriente



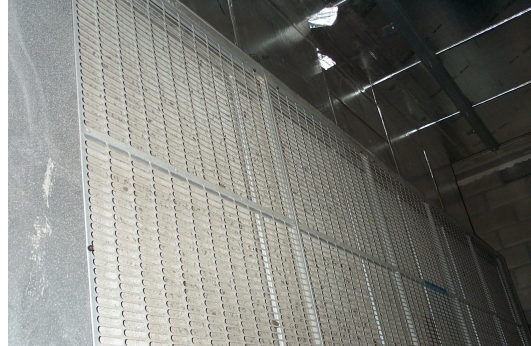
$$hA^* = \frac{hA \text{ en } C_{min}}{hA \text{ en } C_{max}} \quad (\text{normalmente } 1)$$

16

XVIII.- INTERCAMBIADORES DE CALOR MÉTODO DE LA EFICIENCIA

XVIII.7.- INTERCAMBIADORES COMPACTOS

Intercambiadores líquido-gas (con mezcla a la salida)



$$Re = \frac{G^* d_H}{\eta} \quad d_H = 4 \frac{L A_{\min}}{A}$$

hc depende de la forma de la aleta (lisa, ondulada, ...)

Se aproxima por la de la batería de tubos liso